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Reg. No. :

**Question Paper Code : 90417**

B.E./B.Tech. DEGREE EXAMINATIONS, NOVEMBER/DECEMBER 2022.

Fifth Semester

Computer Science and Engineering

CS 8501 — THEORY OF COMPUTATION

(Common to : Computer Science and Business Systems)

(Regulations 2017)

Time : Three hours

Maximum : 100 marks

Answer ALL questions.

PART A — (10 × 2 = 20 marks)

1. Prove:  $1 + 2 + \dots + n = n(n+1)/2$  using mathematical induction.
2. Define:  $\varepsilon$ -closure of a state.
3. State: Pumping lemma for regular languages.
4. Consider the following languages.  $L_1 = \{ab, abb, abbb, \dots\}$  and  $L_2 = \Phi$  (empty language). Identify the list of strings that are part of the language created by  $L_1.L_2 \cup L_2^*$
5. When do you say that given grammar G is ambiguous?
6. Draw a PDA to accept strings of the language,  $L = \{a^n cb^n \mid n \geq 0\}$
7. What is the necessity of forming normal forms of an CFG?
8. List the properties of CFL that are closed.
9. Define "Non-Recursive" languages.
10. Write the significance of NP problems.

PART B — (5 × 13= 65 marks)

11. (a) Draw a Deterministic Finite Automata recognizing the language containing string that are multiples of 4 when represented in binary. Test your DFA using any two strings of the language.

Or

- (b) Draw a Deterministic Finite Automata recognizing the language corresponding to the regular expression  $(a + bca^*)^*$ . Test your DFA using any two strings of the language.
12. (a) Prove the following statement with justification.  
"The language  $L = \{a^i b^j c^k \mid i, j > 0\}$  is not regular".

Or

- (b) Minimize the given automata, G. [Refer Figure. 12(b)]

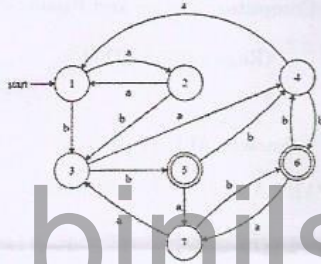


Figure. 12(b)

13. (a) Examine whether the language,  $L = \{a^n b^p c^n d^{2p} \mid n > 0\}$  can be designed using Pushdown automation. Justify your answer.

Or

- (b) Examine whether the language,  $L = \{a^{2n} b^p c^{2n} \mid n > 0\}$  can be designed using Pushdown automation. Justify your answer.
14. (a) Convert the following grammar to be in Chomsky Normal Form.

$S \rightarrow AaA$   
 $A \rightarrow aaBa \mid CDA \mid CD$   
 $B \rightarrow bB$   
 $C \rightarrow Ca \mid D$   
 $D \rightarrow bD \mid \epsilon$

Or

- (b) Design a Turing machine to perform the following function,  
 $f(x) = 2x + 2, x > 0$ .

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15. (a) State and prove the halting problem.

Or

(b) State whether the instances of the Post Correspondence Problem (PCP) have a solution. The following are the instances with  $\Sigma = \{0,1\}$ .

Index	List A	List B
1	10	01
2	110	011
3	110	01
4	000	00
5	10	010

In case the PCP has a solution, describe the post-correspondence solution with justification.

PART C — (1 × 15 = 15 marks)

16. (a) Identify the type of grammar as per Chomsky's hierarchy and design an appropriate automation model.

$S \rightarrow aSBC$       $S \rightarrow aBC$   
 $CB \rightarrow BC$       $aB \rightarrow ab$   
 $bB \rightarrow bb$       $bC \rightarrow bc$   
 $cC \rightarrow dd$

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Or

(b) Identify the type of grammar as per Chomsky's hierarchy and design an appropriate automation model.

$S \rightarrow aSBC$       $S \rightarrow aBC$   
 $CB \rightarrow BC$       $aB \rightarrow ab$   
 $bB \rightarrow bb$       $bC \rightarrow bcc$   
 $cC \rightarrow cccc$