

PROPERTIES OF PURE SUBSTANCE 1

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Properties of pure substance and steam power cycle
Properties of pure substance (water, air)
and
steam power cycles.

Pure substance is a substance which has a fixed chemical composition, throughout its mass.

Formation of steam:

(01)
Phase change process of pure substances:



$$h_w = h_f + x h_{fg}$$

$$h_g = h_f + h_{fg}$$

$$h_{sup} = h_g + C_p (T_{sup} - T_{sat})$$



Consider One kg of ice in a closed vessel under a pressure of p and at a temp. of -20°C . If the ice is gradually heated when the pressure remains constant, the following changes will occur.

- (a) The temperature of the ice will increase till it reaches the freezing temperature of water at 0°C . It is shown by the line 1-2.
- (b) On further heating beyond point 2, there is no rise in temp. till the whole of the ice has been melted and converted into water. This process is represented by the line 2-3. The heat added during the period is called Latent heat of Ice.
- (c) On further heating, the water reaches its boiling point or saturation point 4. The amount of heat added during heating of water from 0°C to saturation temp. of 100°C is known as sensible heat.
- (d) On further heating beyond 4, the water will gradually be converted into steam when the temp remains constant. The same process continues till all water particles converted into wet steam. The line 4-4' represents this process.
- (e) If the wet steam is further heated, wet steam is converted into dry steam.
- (f) When the dry steam is further heated, the temperature rises again. This process is called super heating and the steam obtained is known as superheated steam.

Dryness fraction: (x)

$$x = \frac{m_g}{m_f + m_g}$$

m_g - mass of dry steam in kg
 m_f - mass of water vapour.

This term (x) applicable only for wet steam.

for dry steam $m_f = 0$

so $x = 1$ for dry steam.

Wetness fraction:
$$= \frac{m_f}{m_f + m_g}$$

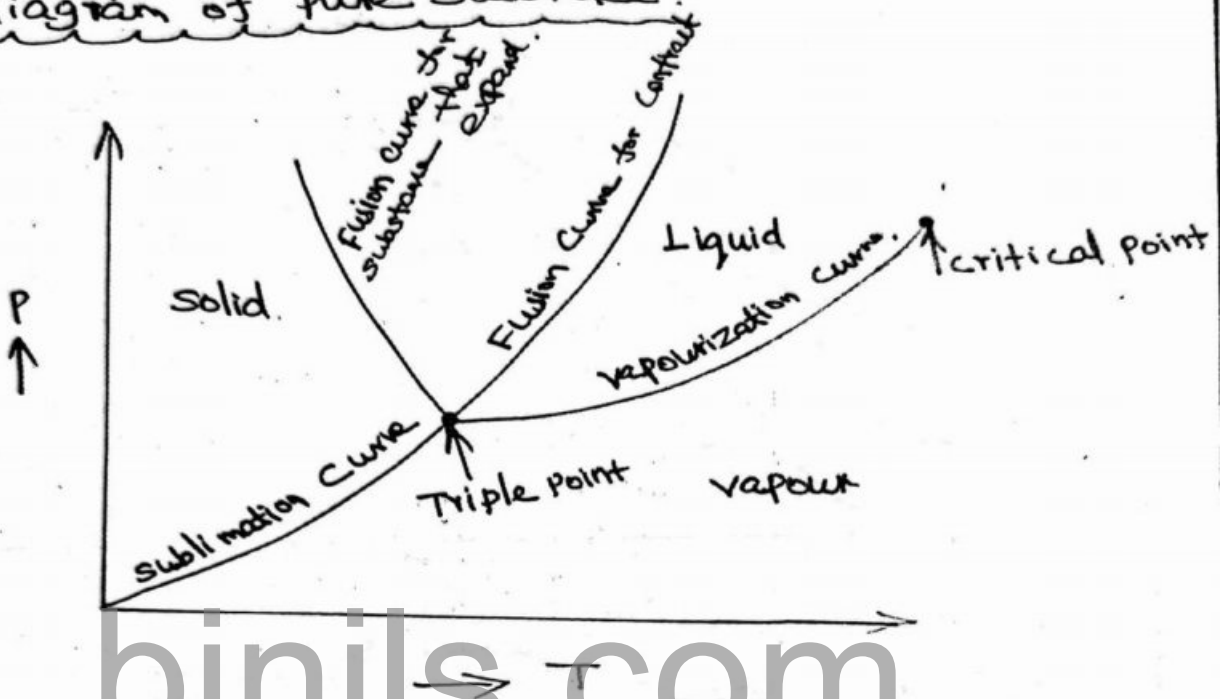
Wetness fraction = $1 - x$

Phase Rule (or) Gibbs Phase Rule

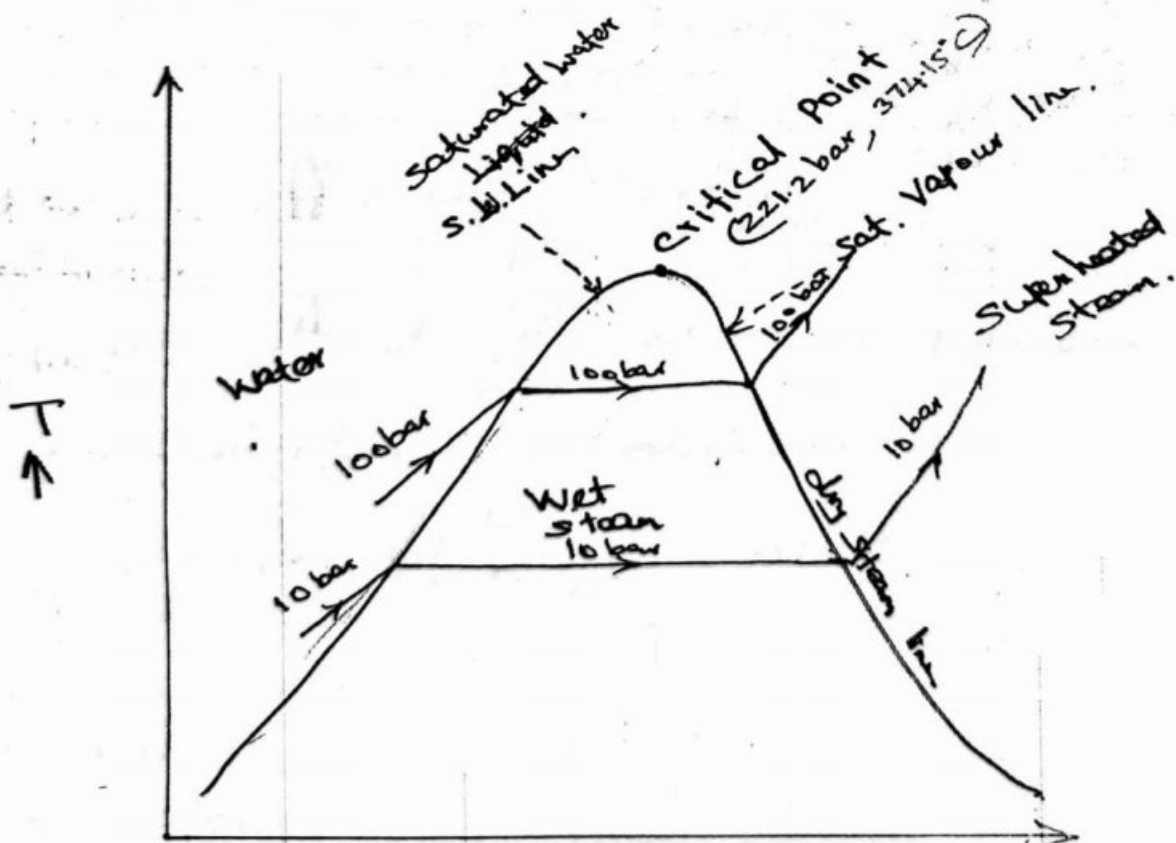
$$n = C - \phi + 2$$

- n - The no. of independent variables.
- C - The no. of components
- ϕ - The no. of phases.

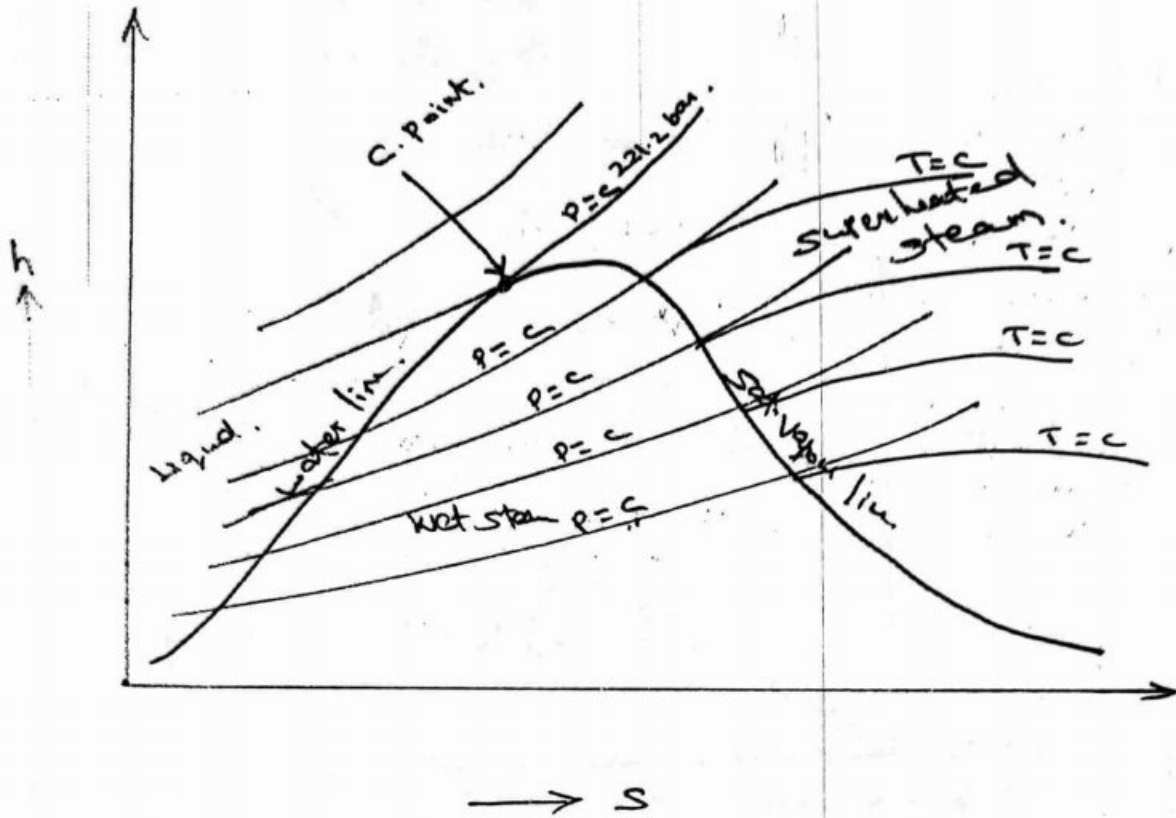
P-T diagram of pure substance:



T-s diagram of pure substance:



h-s diagram (ot) chart



Types of steam:

- ① wet steam
- ② dry steam
- ③ super heated steam.

x = dryness fraction

x = (0 to 1)

"x" values	Substance Condition	Enthalpy (h)	Entropy (S)
If x = 0	Water	$h = h_f$	$S = S_f$
If x = 0.1 - 0.99	Wet steam	$h_{wet} = h_f + x h_{fg}$	$S_{wet} = S_f + x S_{fg}$
If x = 1	dry steam	$h_{dry} = h_f + h_{fg} = h_g$	$S_{dry} = S_f + S_{fg} = S_g$
—	Superheated steam	$h_{sup} = h_g + c_p (T_{sup} - T_s)$	$S_{sup} = S_g + c_p \log \left(\frac{T_{sup}}{T_s} \right)$

T_{sup} - super heated Temp.
 T_s - saturated Temp.
 c_p - specific heat of steam

Properties	Wet steam	dry steam	superheated steam.
Enthalpy (h) KJ/kg	$h_{wet} = h_f + x h_{fg}$	$h_{dry} = h_g = h_f + h_{fg}$	$h_{sup} = h_g + C_{p_s} (T_{sup} - T_s)$
Entropy (s) KJ/kg K	$s_{wet} = s_f + x s_{fg}$	$s_{dry} = s_g = s_f + s_{fg}$	$s_{sup} = s_g + C_{p_s} \ln \left(\frac{T_{sup}}{T_s} \right)$
Sp. Volume (v) m ³ /kg	$v_{wet} = x v_g$	$v_{dry} = v_g$	$v_{sup} = v_g \left(\frac{T_{sup}}{T_s} \right)$
Density (ρ) kg/m ³	$\rho_{wet} = \frac{1}{v_{wet}}$	$\rho_{dry} = \frac{1}{v_g}$	$\rho_{sup} = \frac{1}{v_{sup}}$
Work done (W) KJ/kg	$W_{wet} = 100 P v_{wet}$	$W_{dry} = 100 P v_g$	$W_{sup} = 100 \times P v_{sup}$
Internal energy (u) KJ/kg	$u_{wet} = h_{wet} - W_{wet}$	$u_{dry} = h_{dry} - W_{dry}$	$u_{sup} = h_{sup} - W_{sup}$

$h = u + Pv$
 $u = h - Pv$
 $h = u + Pv$

Systems	Work done	Heat transfer
Boiler	$W = 0 \checkmark$	$Q = h_2 - h_1$
Turbine	$W = h_2 - h_1$	$Q = 0$
Condenser	$W = 0 \checkmark$	$Q = h_1 - h_2$
Nozzle	$W = 0 \checkmark$	$Q = 0$

Steam Table:

Table 1 - Temp. Table.

Table 2 - Pressure Table.

Table 3 - sp. vol. of superheated

Table 4. Sp. enthalpy

Table 5. Sp. entropy

Table 1
Temperature Tables

Temp	P _{sat}	sp. vol.		sp. enthalpy		sp. entropy	
		v _g	v _f	h _g	h _f	s _g	s _f
0	-	-	-	-	-	-	-
1	-	-	-	-	-	-	-
2	-	-	-	-	-	-	-
3	-	-	-	-	-	-	-
4	-	-	-	-	-	-	-

Table 3
sp. volume m³/kg

P _{sat} bar	T _s °C	100	150	200	250	---
0.02	17.5					
0.04	29.0					
0.06	36.2					
0.08						
0.10						

1. Determine the condition of steam at a temp. of 220°C and enthalpy of 2750 kJ/kg.

G.D
 $T = 220^\circ\text{C}$
 $h = 2750 \text{ kJ/kg}$

Wet \rightarrow dry steam \rightarrow Superheated
 $h_{wet} < h_g < h_{super}$

dry steam - 2 new eq. (1) & (2)
 value h_g value at 6 eq. (1) & (2)
 give enthalpy value
 h_g value
 2799.9 kJ/kg
g - dry steam

To find: condition of steam.
 wet (or) dry (or) superheated

- Solution:
 From steam table at 220°C
 $h_g = 2799 \text{ kJ/kg}$
 • $h < h_g \Rightarrow$ wet steam.
 • $h = h_g \Rightarrow$ dry steam.
 • $h > h_g \Rightarrow$ superheated steam.

$h < h_g$ so the steam condition is Wet

Ques:

$h_{wet} = 2750 \text{ kJ/kg}$
 $x = ?$
 $h_{wet} = h_f + x h_{fg}$

Table 1
 Temp. T_{sat}
 bar v_f v_g h_f h_g h_{fg}

220°C	23.18	0.001	943.7	2799.9	1856.2
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From steam table at 220°C
 $h_f = 943.7 \text{ kJ/kg}$
 $h_{fg} = 1856.2 \text{ kJ/kg}$

$2750 = 943.7 + x(1856.2)$

$x = 0.973$

2. Find the specific volume and enthalpy of steam at 9 bar when the steam condition is (a) wet with dryness fraction 0.95 (b) dry saturated (c) superheated and the temp. of steam is 240°C.

G.D:
 $P = 9 \text{ bar}$
 (a) wet steam with $x = 0.95$
 (b) dry steam.
 (c) superheated steam $T_{sup} = 240^\circ\text{C}$.

To find: v , h

From steam table at 9 bar.

$$T_s = 175.4^\circ\text{C}$$

$$V_f = 0.00121 \text{ m}^3/\text{kg}$$

$$V_g = 0.21482 \text{ m}^3/\text{kg}$$

$$h_f = 742.6 \text{ kJ/kg}$$

$$h_{fg} = 2029.5 \text{ kJ/kg}$$

$$h_g = 2772.1 \text{ kJ/kg}$$

Table 2.
Pressure Tables

P, bar	T _s , °C	V _f	V _g	h _f	h _{fg}	h _g
9	175.4	0.00121	0.21482	742.6	2029.5	2772.1

(a) Wet steam: $x = 0.95$.

sp. volume $V_{wet} = x V_g = 0.95 \times 0.21482 = 0.204 \text{ m}^3/\text{kg}$

Enthalpy $h_{wet} = h_f + x h_{fg} = 742.6 + 0.95(2029.5) = 2670.6 \text{ kJ/kg}$

(b) dry steam:

$$V_{dry} = V_g = 0.21482 \text{ m}^3/\text{kg}$$

$$h_{dry} = h_g = 2772.1 \text{ kJ/kg}$$

(c) super heated steam: $T_{sup} = 240^\circ\text{C}$

$$V_{sup} = V_g \left(\frac{T_{sup}}{T_s} \right) = 0.21482 \left(\frac{240 + 273}{175.4 + 273} \right) = 0.2157 \text{ m}^3/\text{kg}$$

$$h_{sup} = h_g + C_{ps} (T_{sup} - T_s)$$

$h_{sup} = ?$ From super heated steam Table at 9 bar and 240°C

$200^\circ\text{C} - 2832.7 \text{ kJ/kg}$

$250^\circ\text{C} - 2946.8 \text{ kJ/kg}$

P ₁	T _s	100°C	150°C	200°C	250°C
9	175.4				
6					
7					
8					
9	175.4			2832.7	2946.8

Interpolation method

$$= 2832.7 + \frac{(2946.8 - 2832.7)}{250 - 200} (240 - 200)$$

$$h_{sup} = 2923.98 \text{ kJ/kg}$$

3. 2 kg of steam initially at 5 bar and 0.6 dry is heated at constant pressure until the temperature becomes 350°C . Find the change in entropy and internal energy.

G.D:

$$m = 2 \text{ kg}$$

$$P_1 = 5 \text{ bar}$$

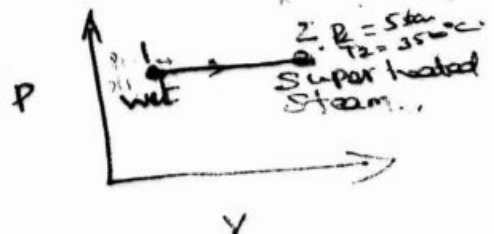
$$x_1 = 0.6$$

$$T_2 = 350^\circ\text{C}$$

① Constant pressure process

$$P_1 = P_2 = 5 \text{ bar}$$

To find: $\Delta S = m(S_2 - S_1)$
 $\Delta U = m(U_2 - U_1)$



Solution:

From steam Table at 5 bar
 $T_s = 151.8^\circ\text{C}$
 $T_2 > T_s$ so the final condition is Superheated steam.

1 $T_2 > T_s \Rightarrow$ Super
 1 $T_2 = T_s =$ dry
 2 $T_2 < T_s =$ wet
 $T_s - \text{sat. temp. of dry steam}$
 Temp.

(i) Change in entropy:

$$\Delta S = m(S_2 - S_1)$$

$$\Delta S = m(S_{\text{sup.}} - S_{\text{wet}})$$

$$S_{\text{wet}} = S_f + x \cdot S_{fg}$$

From steam table at 5 bar.

$$S_f = 1.86 \text{ kJ/kgK}$$

$$S_{fg} = 4.959 \text{ kJ/kgK}$$

$$S_{\text{wet}} = 1.86 + 0.6(4.959) = 4.835 \text{ kJ/kgK}$$

$S_{\text{sup.}} = ?$
 From superheated steam (table-5) at 5 bar and 35°C

$$S_{\text{sup.}} = 7.634 \text{ kJ/kgK}$$

$$\Delta S = m(S_{\text{sup.}} - S_{\text{wet}})$$

$$= 2(7.634 - 4.835)$$

$$\Delta S = 5.598 \text{ kJ/K}$$

(ii) change in internal energy:

$$\Delta U = m(U_2 - U_1)$$

$$\Delta U = m(U_{\text{sup.}} - U_{\text{wet}})$$

$$U_{\text{wet}} = h_{\text{wet}} - W_{\text{wet}}$$

$$= h_f + x h_{fg} - 100 p v_{\text{wet}}$$

$$= h_f + x h_{fg} - 100 p x v_g$$

From steam table at 5 bar

$$h_f = 640.1 \text{ kJ/kg}$$

$$h_{fg} = 2007.4 \text{ kJ/kg}$$

$$v_g = 0.37466 \text{ m}^3/\text{kg}$$

$$U_{\text{wet}} = 640.1 + 0.6(2007.4) - 100 \times 5 \times 0.6 \times 0.37466$$

$$U_{\text{wet}} = 1798.54 - 112.398$$

$$U_{\text{wet}} = 1798.142 \text{ kJ/kg}$$

$$U_{sup} = h_{sup} - W_{sup}$$

$$U_{sup} = h_{sup} - 100 P V_{sup}$$

$h_{sup} = ?$
From Superheated Steam (Table-4) at 5 bar and 350°C

$$h_{sup} = 3168.1 \text{ kJ/kg}$$

$x_{sup} = ?$
From Superheated steam (Table-3) at 5 bar and 350°C

$$v_{sup} = 0.5701 \text{ m}^3/\text{kg}$$

$$U_{sup} = 3168.1 - 100 \times 5 \times 0.5701$$

$$U_{sup} = 2823.05 \text{ kJ/kg}$$

$$\Delta U = m(U_{sup} - U_{wet})$$

$$= 2(2823.05 - 1792.142)$$

$$\Delta U = 2051.816 \text{ kJ}$$

$$\Delta U = 2181.816 \text{ kJ}$$

4.

Steam at 0.8 MPa, 250°C and flowing at the rate of 1 kg/s passes into a pipe carrying wet steam at 0.8 MPa, 0.95 dry. After adiabatic mixing the flow rate is 2.3 kg/s.

Determine the properties of the steam after mixing. (Nov-04, Nov-12).

G.D:

$$P_1 = 0.8 \text{ MPa} = 8 \text{ bar } T_1 = 250^\circ\text{C}$$

$$T_1 = 250^\circ\text{C}$$

$$m_1 = 1 \text{ kg/s}$$

$$P_2 = 0.8 \text{ MPa} = 8 \text{ bar}$$

$$x_2 = 0.95$$

$$m_3 = 2.3 \text{ kg/s}$$

To find:

$$h_3, s_3 = ?$$

Solution:

mass of steam before mixing = mass of steam after mixing.

$$m_1 + m_2 = m_3$$

$$1 + m_2 = 2.3$$

$$m_2 = 1.3 \text{ kg/s}$$

Energy Balance eqn:

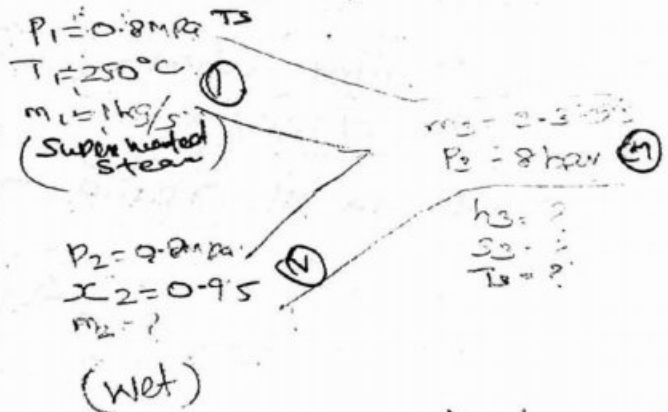
$$m_1 h_1 + m_2 h_2 = m_3 h_3$$

From steam table at 8 bar and

$$T_g = 170.4^\circ\text{C}$$

$T_1 > T_g$ So the steam condition

at point 1 is superheated steam.



$$m_1 h_{sup} + m_2 h_{wet} = m_3 h_3$$

$h_{sup} = ?$

From superheated steam table - 4 at 8 bar and 250°C

$$h_{sup} = 2950.4 \text{ kJ/kg}$$

$h_{wet} = ?$

$$h_{wet} = h_f + x h_{fg}$$

from steam table at 8 bar

$$h_f = 720.9 \text{ kJ/kg}$$

$$h_{fg} = 2046.5 \text{ kJ/kg}$$

$$h_{wet} = 720.9 + 0.95(2046.5)$$

$$h_{wet} = 2664.27 \text{ kJ/kg}$$

$$1 \times (2950) + 1.3 \times (2664.27) = 2.3 \times (h_3)$$

$$h_3 = 2788.67 \text{ kJ/kg}$$

From steam table at 8 bar

$$h_g = 2767.4 \text{ kJ/kg}$$

wet - dry - super
wet < h_g < super

$h_3 > h_g$ so the steam condition at Point ③ is superheated steam.

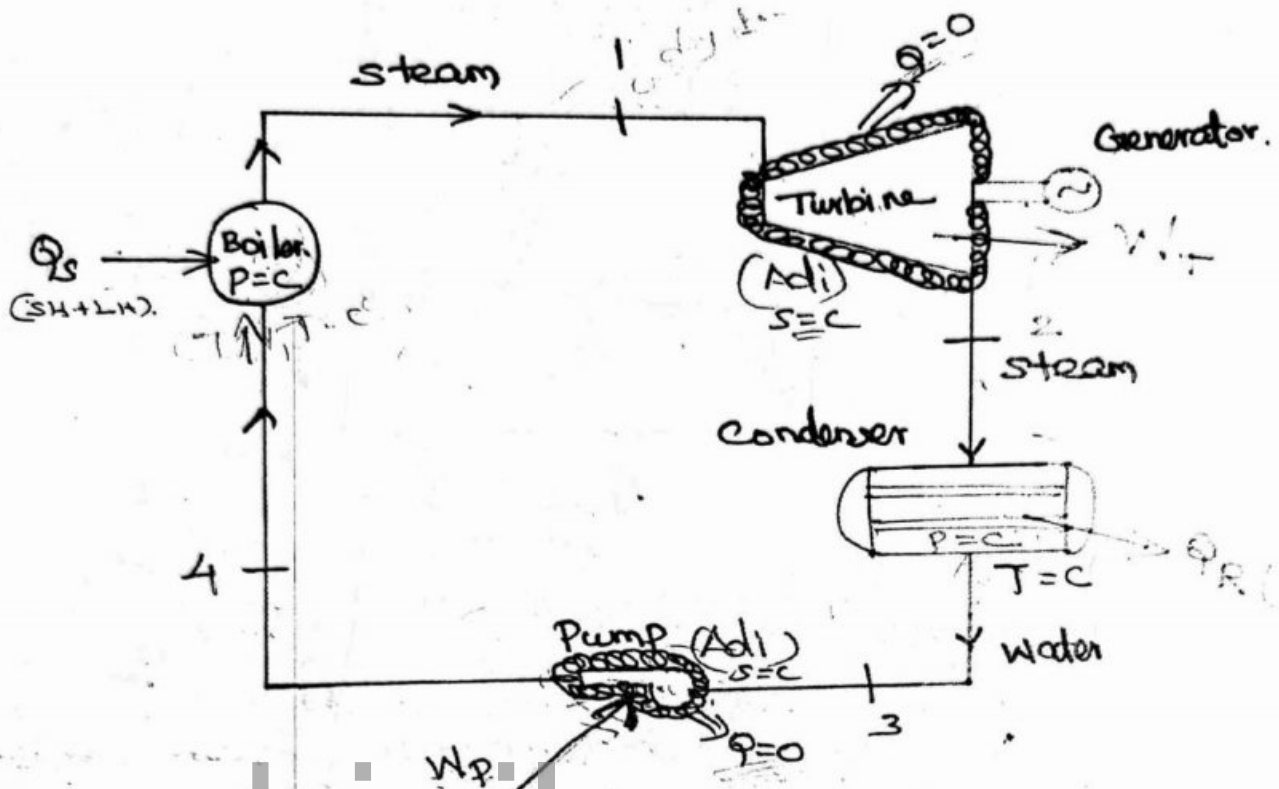
From Mollier chart corresponding to 8 bar and

$$h_3 = 2788.67 \text{ kJ/kg}$$

superheated temp. $T_3 = 180^\circ\text{C}$

Entropy $s_3 = 6.65 \text{ kJ/kgK}$

Steam Power Cycles
(or)
Rankine cycle



1-2 \rightarrow Adiabatic expansion process.

Turbine work done
 $W_T = h_1 - h_2$

2-3 \rightarrow Const. Pr. heat rejection process.

Heat rejection $Q_R = h_2 - h_3$

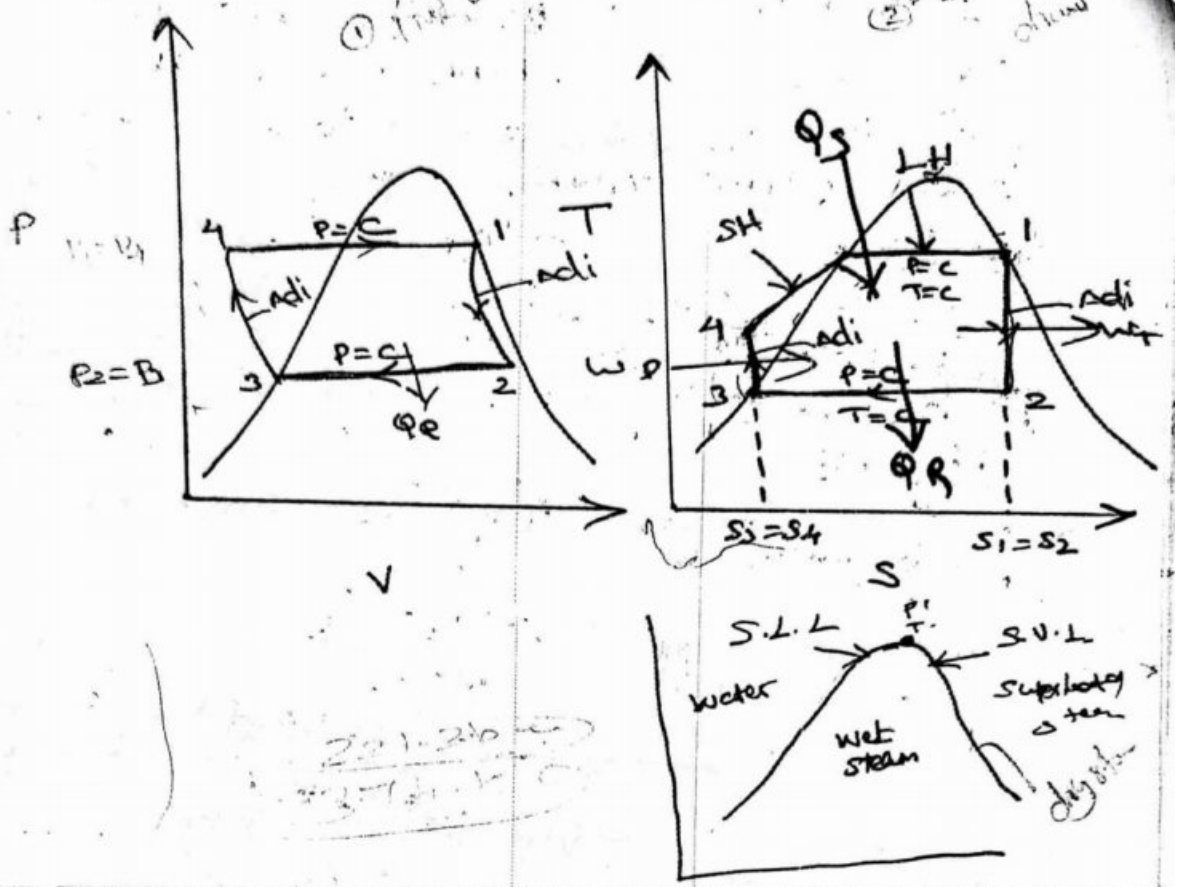
3-4 \rightarrow Adiabatic compression process

$W_p = h_4 - h_3 \Rightarrow \begin{cases} W_p = \frac{V_3}{\gamma} (P_4 - P_3) \\ W_p = \gamma V_3 (P_1 - P_2) \end{cases}$ $W = PV$
 $P_1 = P_4$
 $P_2 = P_3$

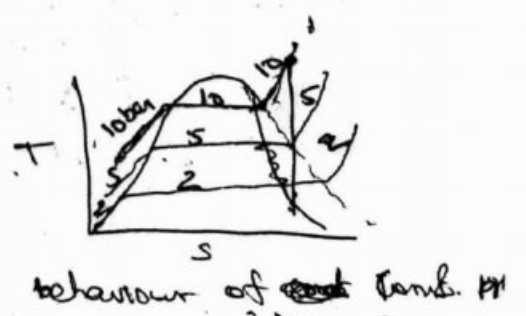
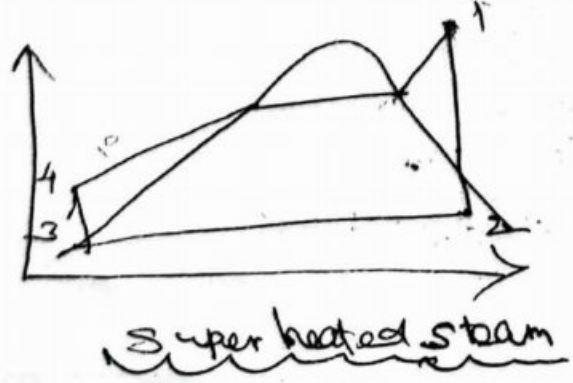
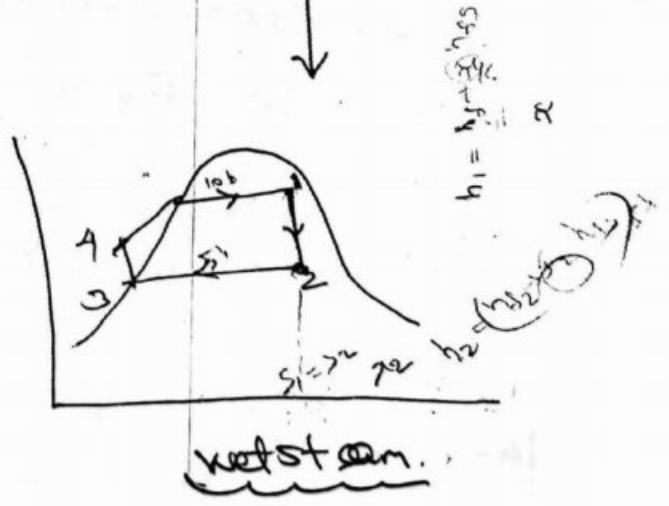
4-1 \rightarrow Const. Pr. heat supplied process.

$Q_s = h_1 - h_4$
Work done $W = W_T - W_p$ (or) $Q_s - Q_R$
 $\eta = \frac{W}{Q_s} = \frac{W_T - W_p}{Q_s} = \frac{(h_1 - h_2) - (h_4 - h_3)}{h_1 - h_4}$

(or)
 $\eta = \frac{W}{Q_s} = \frac{Q_s - Q_R}{Q_s} = \frac{(h_1 - h_4) - (h_2 - h_3)}{(h_1 - h_4)}$

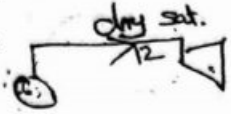


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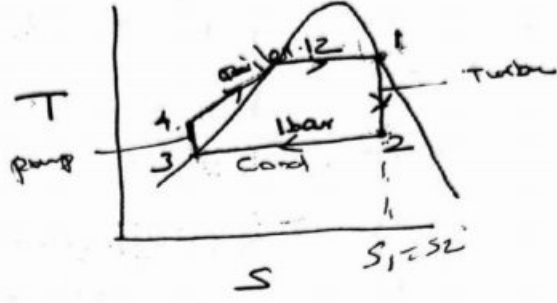
1. 10/11/21

1. Dry saturated steam is supplied to a steam turbine at 12 bar and after the expansion its condenser pressure is 1 bar. Find the Rankine cycle efficiency, specific steam consumption, neglect feed pump work.



G.P.:

Dry saturated steam
 $P_1 = 12 \text{ bar}$ (Turbine pr.)
 $P_2 = 1 \text{ bar}$ (cond. pr.)



To find:

$$\eta_{\text{Rankine}} = \frac{W}{Q_s} = \frac{W_T - W_P}{Q_s}$$

$$= \frac{(h_1 - h_2) - W_P}{h_1 - h_4}$$

$$= \frac{(h_1 - h_2) - W_P}{h_1 - (h_3 + W_P)}$$

$$W_P = h_4 - h_3$$

$$h_4 = h_3 + W_P$$

Neglect the pump work

$$\eta_{\text{Rankine}} = \frac{h_1 - h_2}{h_1 - h_3}$$

$h_1, h_2, h_3 = ?$

$h_1 = ?$ At point 1 steam condition is dry

$$h_1 = h_g$$

From steam table at 12 bar

$$h_g = 2782.7 \text{ kJ/kg} \quad s_f = s_g = 6.529 \text{ kJ/kgK}$$

$$h_1 = h_g = 2782.7 \text{ kJ/kg}$$

$h_2 = ?$ At point 2 steam condition is wet (x_2)

$$h_2 = (h_{f2} + x_2 h_{fg2})_{1 \text{ bar}}$$

$x_2 = ?$

$$(s_1)_{\text{dry}} = (s_2)_{\text{wet}}$$

$$(s_g)_{12 \text{ bar}} = (s_{f2} + x_2 s_{fg2})_{1 \text{ bar}}$$

$$6.529 = (s_{f2} + x_2 s_{fg2})_{1 \text{ bar}}$$

From steam table at 1 bar

$$s_f = 1.3026 \text{ kJ/kgK} \quad h_f = 417.46 \text{ kJ/kg}$$

$$s_{fg} = 6.0574 \text{ " } \quad h_{fg} = 2258.9 \text{ "}$$

$$6.529 = 1.3026 + x_2 (6.0574)$$

$$x_2 = 0.86 \checkmark$$

$$h_2 = h_{f2} + x_2 h_{g2} = 417.5 + 0.1797(2257.6) = 2359.66 \text{ kJ/kg}$$

$$h_2 = 2359.66 \text{ kJ/kg}$$

$h_3 = ?$

At Point 3 steam condition is fluid (f)

$h_3 = (h_{f3})_{1 \text{ bar}} = h_{f2}$ at steam table at 1 bar h_f

$$h_{f3} = h_3 = 417.5 \text{ kJ/kg}$$

$$\eta_{\text{Rankine}} = \frac{h_1 - h_2}{h_1 - h_3} = \frac{2782.7 - 2359.66}{2782.7 - 417.5} \times 100$$

$$\eta = 0.1797 = 17.97\% \checkmark$$

S.S. consumption: $SSC = \frac{3600}{W} = \frac{3600}{h_1 - h_2}$

$$= \frac{3600}{2782.7 - 2359.66}$$

$$SSC = 8.46 \text{ kJ/kw-hr}$$

2. A steam boiler generates steam at 30 bar, 300°C at the rate of 2 kg/s. This steam is expanded isentropically in a turbine to a condenser pressure of 0.05 bar, condensed at constant pressure and pumped back to boiler.

- Draw the T-s diagram of Rankine cycle.
- Find heat supplied in the boiler per hr.
- Determine the quality of steam after expansion.
- What is the power generated by the turbine.
- Find Rankine cycle efficiency.

To find: Q_s, x_2, W_T, η

Q_s, x_2, W_T, η

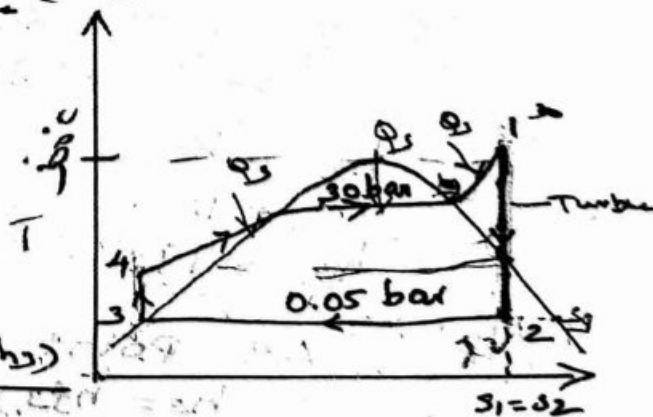
Heat supplied $Q_s = h_1 - h_4$

$P_1 = 30 \text{ bar}$
 $T_1 = 300^\circ \text{C}$

$$W_T = h_1 - h_2$$

$$\eta_{\text{Rankine}} = \frac{W}{Q_s} = \frac{W_T - W_P}{Q_s}$$

$$\eta = \frac{(h_1 - h_2) - (h_4 - h_3)}{h_1 - h_4}$$



$$s_2 = s_3 = s_4 = s_1$$

$$s_2 < s_g = \text{wet}$$

Solution:

$h_1, h_2, h_3, h_4 = ?$

$h_1 = ?$ At point 1 steam condition is superheated.

From steam table at 30 bar
 $T_s = 233.8^\circ\text{C}$ (saturated temp (or) dry steam temp).

$T_1 > T_s$ so the steam condition is

Superheated steam.

From superheated steam Table - at 30 bar, 300°C

$h_1 = 2995 \text{ kJ/kg}$ $s_1 = 6.542 \text{ kJ/kgK}$

$h_2 = ?$

At point 2 steam condition is Wet steam.
 $s_1 = s_2 = 6.542 \text{ kJ/kgK}$

From steam table at 0.05 bar
 $s_g = 8.396 \text{ kJ/kgK}$

$s_2 < s_g$ so the steam condition is Wet.

$h_2 = h_{f2} + x_2 h_{fg2}$

$x_2 = ?$

$s_1 = s_2$

$(s_1)_{\text{sup 30 bar}} = (s_2)_{\text{wet 0.05 bar}}$

$6.542 = (s_{f2} + x_2 s_{fg2})_{0.05}$

From steam table at 0.05 bar.

$s_f = 0.476 \text{ kJ/kgK}$ $h_f = 137.8 \text{ kJ/kg}$

$s_{fg} = 7.920$ $h_{fg} = 2423.8 \text{ kJ/kg}$

$v_f = 0.001005 \text{ m}^3/\text{kg}$

$6.542 = 0.476 + x_2 (7.920)$

$x_2 = 0.766$

$h_2 = h_{f2} + x_2 h_{fg2}$

$= 137.8 + 0.766 (2423.8)$

$h_2 = 1994.3 \text{ kJ/kg}$

$h_3 = ?$ At point 3 steam condition is Saturated.

$h_3 = (h_{f3})_{0.05 \text{ bar}} = 137.8 \text{ kJ/kg}$

$h_4 = ?$

$W_p = h_4 - h_3 = v_3 (P_4 - P_3)$

PV

$h_4 - h_3 = v_{f3} (P_1 - P_2)$

$$h_4 = h_3 + v_{f3} (p_1 - p_2)$$
$$= 137.8 + 0.001005 (30 - 0.05) \times 1000$$

$$h_4 = 140.81 \text{ kJ/kg}$$

(b) Heat supplied $Q_s = m(h_1 - h_4)$

$$= 2(2995.1 - 140.81)$$
$$= 5708.58 \text{ kJ/sec.}$$
$$= 5708.58 \times 3600 =$$
$$Q_s = 20.55 \times 10^6 \text{ kJ/hr}$$

(c) $x_2 = 0.766$

(d) $W_T = m(h_1 - h_2) = 2(2995.1 - 1994.4)$

$$W_T = 2001.34 \text{ kJ/sec}$$

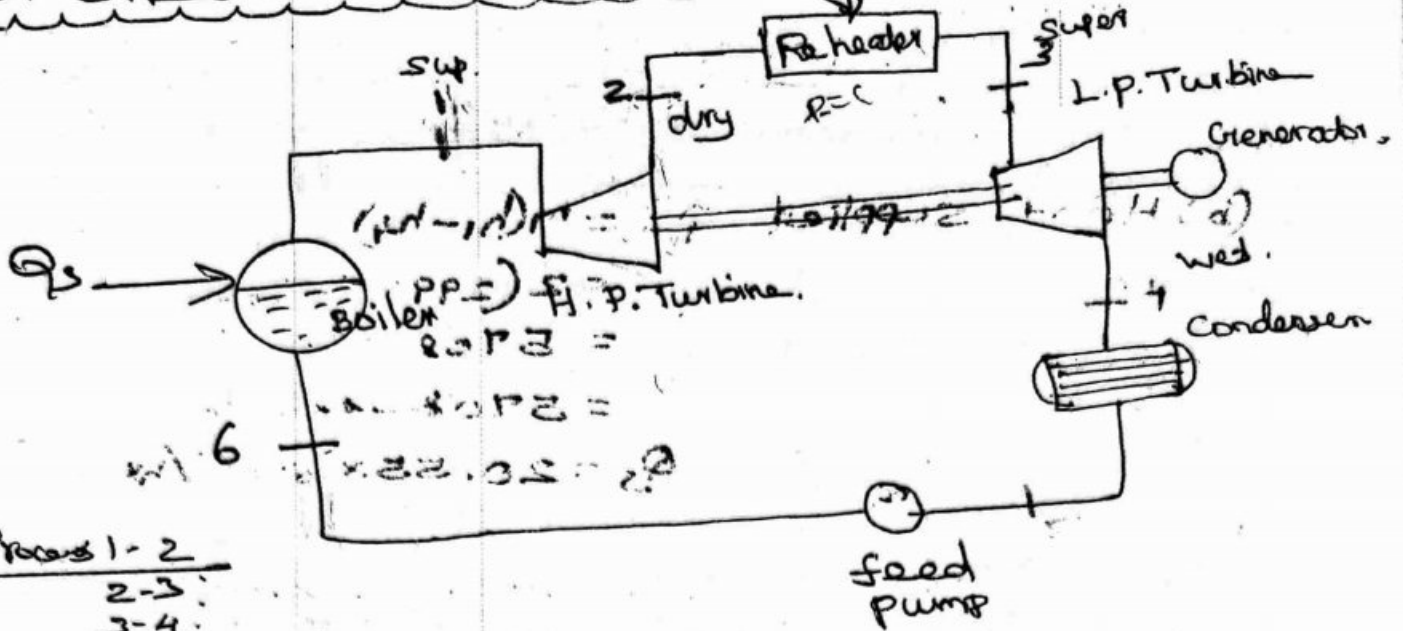
(e) $\eta_{\text{Rankine}} = \frac{W_T - W_P}{Q_s} = \frac{m(h_1 - h_2) - m(h_4 - h_3)}{m(h_1 - h_4)}$

$$= \frac{(2995.1 - 1994.4) - (140.81 - 137.8)}{2995.1 - 140.81} \times 100$$
$$\eta_{\text{Rankine}} = 35\%$$

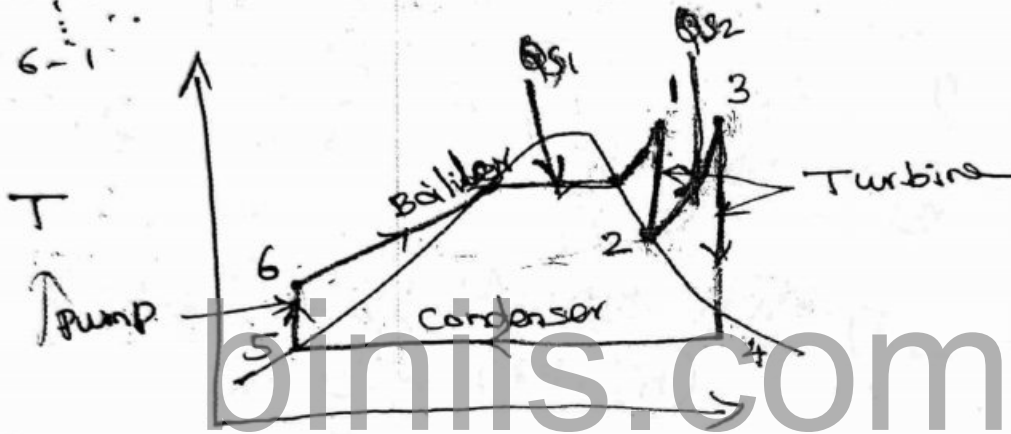
Types of Rankine cycle

- ① Reheat Rankine cycle.
- ② Regenerative Rankine cycle.

Reheat Rankine cycle



Process 1-2
2-3
3-4
4-5
5-6



T-s diagram of Reheat Rankine cycle

$$\eta = \frac{W}{Q_s} = \frac{(W_{T1-2} + W_{T3-4}) - W_p}{(h_1 - h_6) + (h_3 - h_2)}$$

$$\eta = \frac{(h_1 - h_2) + (h_3 - h_4) - (h_6 - h_5)}{(h_1 - h_6) + h_3 - h_2}$$

1. Consider a steam power plant operating on an reheat Rankine cycle. The steam enters the H.P. turbine at 30 bar and 350°C. After expansion to 5 bar, the steam is reheated to 350°C and then expanded the L.P. turbine to the condenser pressure of 0.07 bar. Determine the thermal efficiency of the cycle and the quality of steam at the outlet of the L.P. turbine.

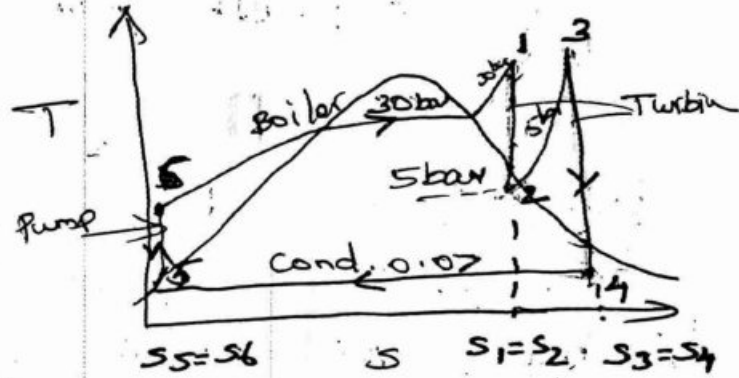
G.D:

$$\left. \begin{aligned} P_1 &= 30 \text{ bar} \\ T_1 &= 350^\circ\text{C} \end{aligned} \right\} \begin{aligned} T_s &= 233.8^\circ\text{C} \\ &\text{Superheated} \\ T_1 &> T_s \end{aligned}$$

$$P_2 = 5 \text{ bar}$$

$$T_3 = 350^\circ\text{C}$$

$$P_4 = 0.07 \text{ bar}$$



To find η , x_4 :

$$\eta = \frac{W_T - W_P}{Q_S} = \frac{W_T - W_P}{Q_S}$$

$$\eta = \frac{(h_1 - h_2) + (h_3 - h_4) - (h_6 - h_5)}{(h_1 - h_6) + (h_3 - h_2)}$$

$h_1, h_2, h_3, h_4, h_5, h_6 = ?$

$h_1 = ?$ At Point 1 steam condition is Superheated.
From superheated steam table at 30 bar and 350°C
 $h_1 = 3117.5 \text{ kJ/kg}$ $s_1 = 6.742 \text{ kJ/kgK}$

$h_2 = ?$ At point 2 steam condition is not.

$$(s_1) = (s_2) = 6.742 \text{ kJ/kgK}$$

From steam table at 5 bar
 $s_g = 6.819 \text{ kJ/kgK}$

$s_2 < s_g$ so the steam condition is not

$$h_2 = h_{f2} + x_2 h_{fg2}$$

$$(s_1)_{\text{sup 30 bar}} = (s_2)_{\text{wet 5 bar}}$$

$$6.742 = (s_{f2} + x_2 s_{fg2})_{5 \text{ bar}}$$

From steam table at 5 bar

$$s_f = 1.860$$

$$h_f = 640.1$$

$$s_{fg} = 4.959$$

$$h_{fg} = 2107.4$$

$$6.742 = 1.860 + x_2(4.959)$$

$$x_2 = 0.98$$

$$h_2 = h_{f2} + x_2 h_{fg2} \\ = 640.1 + 0.98(2107.5)$$

$$h_2 = 2706.56 \text{ kJ/kg}$$

$h_3 = ?$ At point 3 steam condition is Superheated.
 $P_2 = P_3 = 5 \text{ bar} \Rightarrow T_3 = 151.8^\circ\text{C}$
 $T_3 = 350^\circ\text{C}$

$T_3 > T_s$ so the steam condition is superheated.

From Superheated steam Table at 5 bar and 350°C

$$h_3 = 3168.1 \text{ kJ/kg} \quad s_3 = 7.634 \text{ kJ/kgK}$$

$h_4 = ?$ At point 4 steam condition is Wet.

$$s_3 = s_4 = 7.634 \text{ kJ/kgK}$$

From steam Table at 0.07 bar

$$s_g = 8.277 \text{ kJ/kgK}$$

$s_4 < s_g$ so the steam condition is wet

$$h_4 = h_{f4} + x_4 h_{fg4}$$

$$(s_3)_{\text{super}} = (s_4)_{\text{wet 0.07 bar}}$$

$$7.634 = (s_{f4} + x_4 s_{fg4})_{0.07 \text{ bar}}$$

From steam Table at 0.07 bar.

$$s_f = 0.559$$

$$h_f = 163.4$$

$$s_{fg} = 7.718$$

$$h_{fg} = 2409.2$$

$$v_{fg} = 0.001009$$

$$7.634 = 0.559 + x_4(7.718)$$

$$x_4 = 0.91$$

$$h_4 = h_{f4} + x_4 h_{fg4} \\ = 163.4 + 0.91(2409.2)$$

$$h_4 = 2355.772 \text{ kJ/kg}$$

$h_5 = ?$ AT point 5 steam condition is fluid

$$h_5 = (h_{f5})_{0.07 \text{ bar}}$$

From steam table at 0.07 bar.

$$h_5 = h_f = 163.4 \text{ kJ/kg}$$

$h_6 = ?$ AT point 6 steam condition is fluid.

$$W_p = h_6 - h_5 = v_5 (P_6 - P_5) = v_{f5} (P_1 - P_4)$$

$$h_6 - h_5 = 0.001007 (30 - 0.07) \times 100 = 3.013951$$

$$h_6 = 3.013951 + h_5$$

$$= 3.013951 + 163.4$$

$$h_6 = 166.41 \text{ kJ/kg}$$

$$\eta = \frac{(h_1 - h_2) + (h_3 - h_4) - (h_6 - h_5)}{(h_1 - h_6) + (h_3 - h_2)}$$

$$= \frac{(3115.3 - 2706.56) + (3168.1 - 2355.72) - (166.41 - 163.4)}{(3115.3 - 166.41) + (3168.1 - 2706.56)}$$

$$\eta = 35.71\%$$

2) A Reheat cycle operating between 30 and 0.04 bar has a superheat and Reheat temp. of 450°C . The first expansion takes place till the steam is dry saturated and then reheat is given. Neglecting feed pump work. Determine the ideal cycle efficiency.

G1.0

$$P_1 = 30 \text{ bar}$$

$$T_1 = 450^\circ\text{C}$$

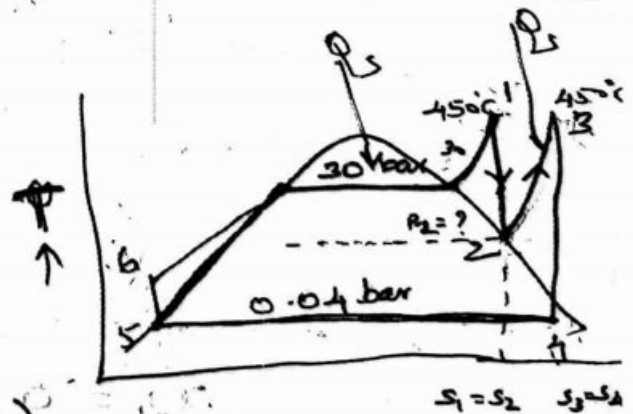
$$P_4 = 0.04 \text{ bar}$$

$$T_3 = 450^\circ\text{C}$$

To find: $\eta = \frac{W}{Q_s} = \frac{W_T - W_p}{Q_s}$

7

$$\eta = \frac{(h_1 - h_2) + (h_3 - h_4)}{(h_1 - h_5) + (h_3 - h_2)}$$



$h_1, h_2, h_3, h_4, h_5 = ?$

$h_1 = ?$ At Point 1 steam condition is superheated

From superheated steam table at 30 bar & 450°C.

$h_1 = 3344.3 \text{ kJ/kg}$ $s_1 = 7.08 \text{ kJ/kgK}$

$h_2 = ?$ At Point 2 steam condition is dry

$h_2 = h_g$ $(s_1) = (s_2) = 7.08 = s_g$ (dry)

From steam table at $s_g = 7.08 \text{ kJ/kgK}$.

Corresponding pressure $P_2 = 2.3 \text{ bar}$.

P	s_g
2.1	7.41
2.2	7.05
2.3	7.08

From steam table at 2.3 bar.

$h_2 = h_g = 2712.6 \text{ kJ/kg} = h_2$

$h_3 = ?$ At Point 3 steam condition is superheated

From superheated steam table at 2.3 bar & 450°C.

$h_3 = 3381.46 \text{ kJ/kg}$ $s_3 = 8.3061 \text{ kJ/kgK}$

$h_4 = ?$ At Point 4 steam condition is wet

$s_3 = s_4 = 8.3061 \text{ kJ/kgK}$

At point 4 $\rightarrow P_4 = 0.04 \text{ bar}$.

From steam table at 0.04 bar.

$s_g = 8.476$

$s_4 < s_g$ so the steam condition is wet

$h_4 = h_{f4} + x_4 h_{fg4}$

$(s_3) = (s_4)$

$8.3061 = s_{f4} + x_4 s_{fg4}$

From steam table at 0.04 bar.

$s_f = 0.423$

$h_f = 121.4$

$s_{fg} = 8.053$

$h_{fg} = 2433.1$

$8.3061 = 0.423 + x_4 (8.053)$

$x_4 = 0.98$

$h_4 = h_{f4} + x_4 h_{fg4}$
 $= 121.4 + 0.98 (2433.1)$

$h_4 = 2505.84 \text{ kJ/kg}$

$h_5 = ?$ At point 5 steam condition is fluid

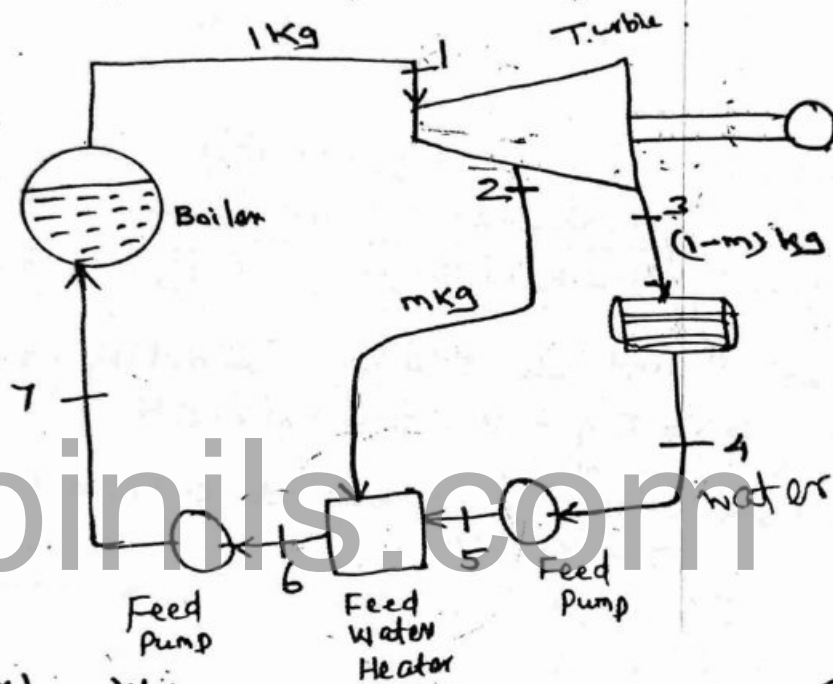
$$h_5 = (h_{f5})_{0.04 \text{ bar.}} = 121.4 \text{ kJ/kg}$$

$$\eta = \frac{(3344.35 - 2712.6) + (3381.46 - 2505.84)}{(3344.35 - 121.4) + (3381.46 - 2712.6)} \times 100$$

$$\eta = 38.73\%$$

2. Regenerative Rankine cycle

- (i) single stage Regenerative cycle
- (ii) Multi " " " "



$$\eta = \frac{W}{Q_s} = \frac{W_T - W_P}{Q_s}$$

$$W_T = 1(h_1 - h_2) + (1-m)(h_2 - h_3)$$

$$W_P = (1-m)(h_5 - h_4) + 1(h_7 - h_6)$$

$$Q_s = 1(h_1 - h_7)$$

$m = ?$

Energy balance eqn.

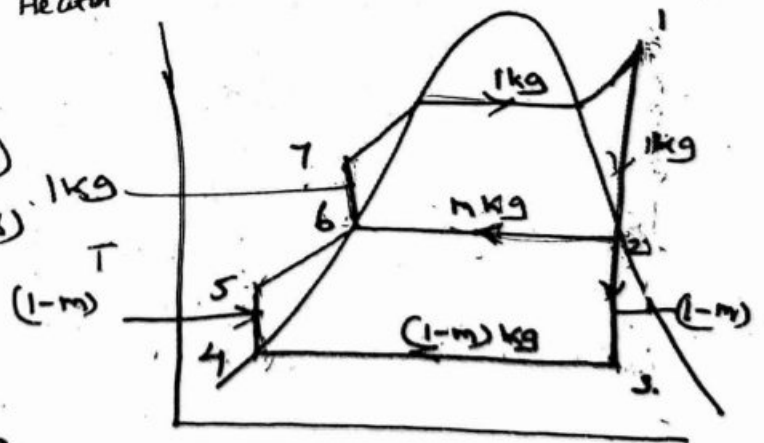
$$m h_2 + (1-m) h_5 = 1(h_6)$$

$$m h_2 + h_5 - m h_5 = h_6$$

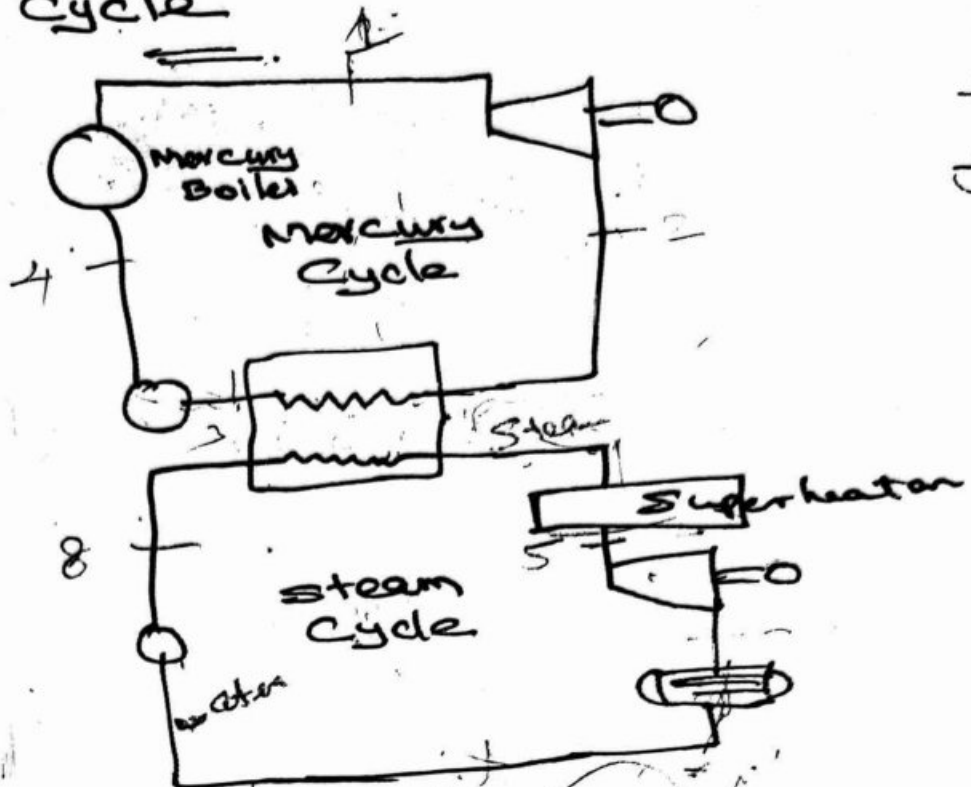
$$m h_2 - m h_5 = h_6 - h_5$$

$$m(h_2 - h_5) = h_6 - h_5$$

$$m = \frac{h_6 - h_5}{h_2 - h_5}$$



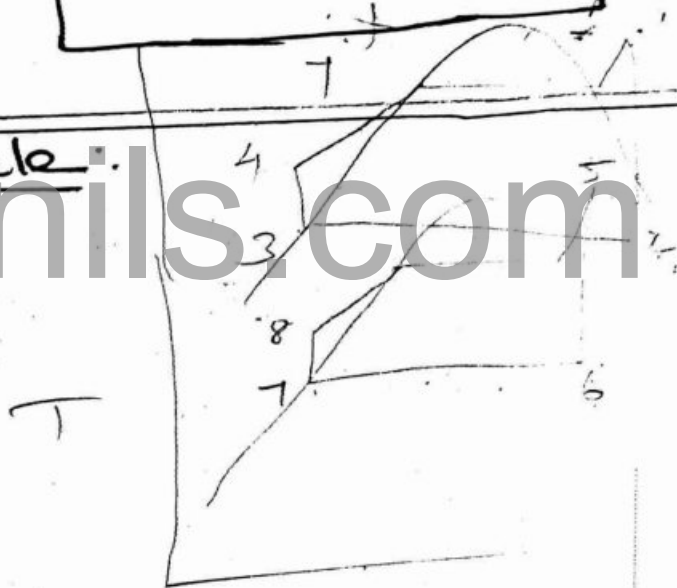
Binary Cycle
Combined Cycle



$$w_T = \frac{h_1 - h_2}{T}$$

Combined cycle.

binils.com



Gas turbine & Steam turbine cycle

