

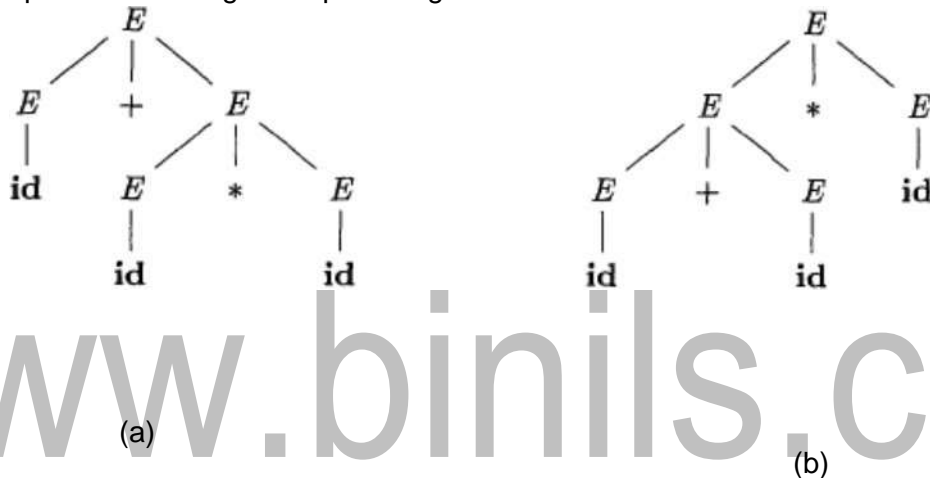
## AMBIGUITY in CFGs

**Definition:** A grammar that produces more than one parse tree for some sentence (input string) is said to be ambiguous.

In other words, an ambiguous grammar is one that produces more than one leftmost derivation or more than one rightmost derivation for the same sentence.

Or If the right hand production of the grammar is having two non terminals which are exactly same as left hand side production Nonterminal then it is said to an ambiguous grammar. Example: If the Grammar is  $E \rightarrow E+E \mid E * E \mid -E \mid (E) \mid id$  and the Input String is  $id + id * id$

Two parse trees for given input string are



Two Leftmost Derivations for given input String are :

$$E \Rightarrow E + E$$

$$\Rightarrow id + E$$

$$\Rightarrow id + E * E$$

$$\Rightarrow id + id * E$$

$$\Rightarrow id + id * id$$

(a)

$$E \Rightarrow E * E$$

$$\Rightarrow E + E * E$$

$$\Rightarrow id + E * E$$

$$\Rightarrow id + id * E$$

$$\Rightarrow id + id * id$$

(b)

The above Grammar is giving two parse trees or two derivations for the given input string so, it is an ambiguous Grammar

**Note:** LL (1) parser will not accept the ambiguous grammars or We cannot construct an LL(1) parser for the ambiguous grammars. Because such grammars may cause the Top Down parser to go into infinite loop or make it consume more time for parsing. If necessary we must remove all types of ambiguity from it and then construct.

**ELIMINATING AMBIGUITY:** Since Ambiguous grammars may cause the top down Parser go into infinite loop, consume more time during parsing.

Therefore, sometimes an ambiguous grammar can be rewritten to eliminate the ambiguity. The general form of ambiguous productions that cause ambiguity in grammars is

$$A \rightarrow A\alpha \mid \beta$$

This can be written as (introduce one new non terminal in the place of second non terminal)

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' \mid \epsilon$$

Example: Let the grammar is  $E \rightarrow E+E \mid E^*E \mid -E \mid (E) \mid id$ . It is shown that it is ambiguous that can be written as

- $E \rightarrow E+E$
- $E \rightarrow E-E$
- $E \rightarrow E^*E$
- $E \rightarrow -E$
- $E \rightarrow (E)$
- $E \rightarrow id$

In the above grammar the 1<sup>st</sup> and 2<sup>nd</sup> productions are having ambiguity. So, they can be written as

$E \rightarrow E+E \mid E^*E$  this production again can be written as

$E \rightarrow E+E \mid \beta$ , where  $\beta$  is  $E^*E$

The above production is same as the general form. so, that can be written as  $E \rightarrow E+T \mid T$   
 $T \rightarrow \beta$

The value of  $\beta$  is  $E^*E$  so, above grammar can be written as

- 1)  $E \rightarrow E+T \mid T$
- 2)  $T \rightarrow E^*E$       **The first production is free from ambiguity** and substitute  $E \rightarrow T$  in the 2<sup>nd</sup> production then it can be written as

$T \rightarrow T^*T \mid -E \mid (E) \mid id$  this production again can be written as

$T \rightarrow T^*T \mid \beta$  where  $\beta$  is  $-E \mid (E) \mid id$ , introduce new non terminal in the Right hand side production then it becomes

$T \rightarrow T^*F \mid F$

$F \rightarrow -E \mid (E) \mid id$       now the entire grammar turned in to it equivalent unambiguous,

**The Unambiguous grammar** equivalent to the given ambiguous one is

- 1)  $E \rightarrow E+T \mid T$
- 2)  $T \rightarrow T^*F \mid F$
- 3)  $F \rightarrow -E \mid (E) \mid id$

**LEFT RECURSION:**

Another feature of the CFGs which is not desirable to be used in top down parsers is left recursion. A grammar is left recursive if it has a non terminal A such that there is a derivation  $A \Rightarrow A\alpha$  for some string  $\alpha$  in  $(TUV)^*$ . LL(1) or Top Down Parsers cannot handle the Left Recursive grammars, so we need to remove the left recursion from the grammars before being used in Top Down Parsing.

The General form of Left Recursion is

$$A \rightarrow A\alpha \mid \beta$$

The above left recursive production can be written as the non left recursive equivalent :

$$\begin{aligned} A &\rightarrow \beta A' \\ A' &\rightarrow \alpha A' \mid \epsilon \end{aligned}$$

Example : - Is the following grammar left recursive? If so, find a non left recursive grammar equivalent to it.

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

Yes ,the grammar is left recursive due to the first two productions which are satisfying the general form of Left recursion, so they can be rewritten after removing left recursion from  $E \rightarrow E + T$ , and  $T \rightarrow T * F$  is

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow +T E' \mid \epsilon \\ T &\rightarrow FT' \\ T' &\rightarrow *F T' \mid \epsilon \\ F &\rightarrow (E) \mid id \end{aligned}$$

#### LEFT FACTORING:

Left factoring is a grammar transformation that is useful for producing a grammar suitable for predictive or top-down parsing. A grammar in which more than one production has common prefix is to be rewritten by factoring out the prefixes.

For example, in the following grammar there are n A productions have the common prefix  $\alpha$ , which should be removed or factored out without changing the language defined for A.

$$A \rightarrow \alpha A1 \mid \alpha A2 \mid \alpha A3 \mid \alpha A4 \mid \dots \mid \alpha An$$

We can factor out the  $\alpha$  from all n productions by adding a new A production and rewriting the A' productions grammar as

$$A \rightarrow \alpha A'$$

$$\begin{aligned} A &\rightarrow \alpha A' \\ A' &\rightarrow A1 \mid A2 \mid A3 \mid A4 \dots \mid An \end{aligned}$$

## BOTTOM-UP PARSING

Bottom-up parsing corresponds to the construction of a parse tree for an input string beginning at the leaves (the bottom nodes) and working up towards the root (the top node). It involves reducing an input string  $w$  to the Start Symbol of the grammar. In each reduction step, a particular substring matching the right side of the production is replaced by symbol on the left of that production and it is the Right most derivation. For example consider the following Grammar:

$$E \rightarrow E+T \mid T$$

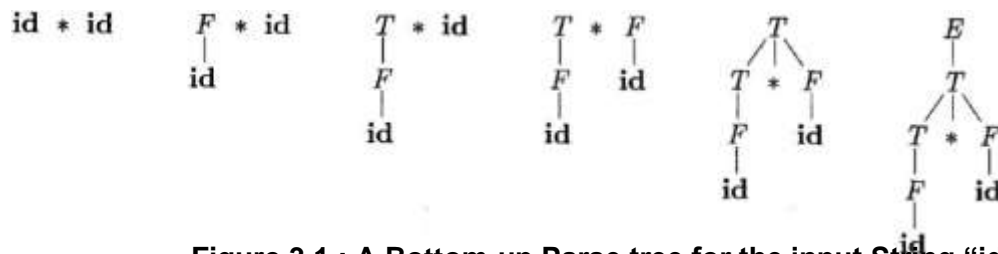
$$T \rightarrow T * F$$

$$F \rightarrow (E) \mid id$$

Bottom up parsing of the input string "id \* id" is as follows:

INPUT STRING	SUB STRING	REDUCING PRODUCTION
id*id	id	$F \rightarrow id$
F*id	T	$F \rightarrow T$
T*id	id	$F \rightarrow id$
T * F	*	$T \rightarrow T * F$
T	T * F	$E \rightarrow T$
E		Start symbol. Hence, the input String is accepted

Parse Tree representation is as follows:



**Figure 3.1 : A Bottom-up Parse tree for the input String "id\*id"**

Bottom up parsing is classified in to 1. Shift-Reduce Parsing, 2. Operator Precedence parsing , and 3. [Table Driven] LR Parsing

- i. SLR(1)
- ii. CALR(1)
- iii. LALR(1)



## LALR (1) Parsing

LALR refers to the lookahead LR. To construct the LALR (1) parsing table, we use the canonical collection of LR (1) items.

In the LALR (1) parsing, the LR (1) items which have same productions but different look ahead are combined to form a single set of items

LALR (1) parsing is same as the CLR (1) parsing, only difference in the parsing table.

Example

### LALR ( 1 ) Grammar

1.  $S \rightarrow AA$
2.  $A \rightarrow aA$
3.  $A \rightarrow b$

Add Augment Production, insert '.' symbol at the first position for every production in G and also add the look ahead.

1.  $S' \rightarrow \bullet S, \$$
2.  $S \rightarrow \bullet AA, \$$
3.  $A \rightarrow \bullet aA, a/b$
4.  $A \rightarrow \bullet b, a/b$

### I0 State:

Add Augment production to the I0 State and Compute the ClosureL

**I0** = Closure ( $S' \rightarrow \bullet S$ )

Add all productions starting with S in to I0 State because "." is followed by the non-terminal. So, the I0 State becomes

**I0** =  $S' \rightarrow \bullet S, \$$   
 $S \rightarrow \bullet AA, \$$

Add all productions starting with A in modified I0 State because "." is followed by the non-terminal. So, the I0 State becomes.

**I0** =  $S' \rightarrow \bullet S, \$$   
 $S \rightarrow \bullet AA, \$$

$A \rightarrow \bullet aA, a/b$

$A \rightarrow \bullet b, a/b$

**I1**= Go to (I0, S) = closure ( $S \rightarrow S\bullet, \$$ ) =  $S \rightarrow S\bullet, \$$

**I2**= Go to (I0, A) = closure ( $S \rightarrow A\bullet A, \$$ )

Add all productions starting with A in I2 State because "." is followed by the non-terminal. So, the I2 State becomes

**I2**=  $S \rightarrow A\bullet A, \$$

$A \rightarrow \bullet aA, \$$

$A \rightarrow \bullet b, \$$

**I3**= Go to (I0, a) = Closure ( $A \rightarrow a\bullet A, a/b$ )

Add all productions starting with A in I3 State because "." is followed by the non-terminal. So, the I3 State becomes

**I3**=  $A \rightarrow a\bullet A, a/b$

$A \rightarrow \bullet aA, a/b$

$A \rightarrow \bullet b, a/b$

Goto (I3, a) = Closure ( $A \rightarrow a\bullet A, a/b$ ) = (same as I3)

Goto (I3, b) = Closure ( $A \rightarrow b\bullet, a/b$ ) = (same as I4)

**I4**= Go to (I0, b) = closure ( $A \rightarrow b\bullet, a/b$ ) =  $A \rightarrow b\bullet, a/b$

**I5**= Go to (I2, A) = Closure ( $S \rightarrow AA\bullet, \$$ ) =  $S \rightarrow AA\bullet, \$$

**I6**= Go to (I2, a) = Closure ( $A \rightarrow a\bullet A, \$$ )

Add all productions starting with A in I6 State because "." is followed by the non-terminal. So, the I6 State becomes

**I6**=  $A \rightarrow a\bullet A, \$$

$A \rightarrow \bullet aA, \$$

$A \rightarrow \bullet b, \$$

Goto (I6, a) = Closure ( $A \rightarrow a\bullet A, \$$ ) = (same as I6)

Goto (I6, b) = Closure ( $A \rightarrow b\bullet, \$$ ) = (same as I7)

**I7**= Go to (I2, b) = Closure ( $A \rightarrow b\bullet, \$$ ) =  $A \rightarrow b\bullet, \$$

**I8**= Go to (I3, A) = Closure ( $A \rightarrow aA\bullet, a/b$ ) =  $A \rightarrow aA\bullet, a/b$

**I9**= Go to (I6, A) = Closure ( $A \rightarrow aA\bullet, \$$ ) =  $A \rightarrow aA\bullet, \$$

If we analyze then LR (0) items of I3 and I6 are same but they differ only in their lookahead.

**I3** = {  $A \rightarrow a\bullet A, a/b$

$A \rightarrow \bullet aA, a/b$

$A \rightarrow \bullet b, a/b$   
}

$I_6 = \{ A \rightarrow a \bullet A, \$$   
 $A \rightarrow \bullet a A, \$$   
 $A \rightarrow \bullet b, \$$   
}

Clearly  $I_3$  and  $I_6$  are same in their LR(0) items but differ in their lookahead, so we can combine them and called as  $I_{36}$ .

$I_{36} = \{ A \rightarrow a \bullet A, a/b/\$$   
 $A \rightarrow \bullet a A, a/b/\$$   
 $A \rightarrow \bullet b, a/b/\$$   
}

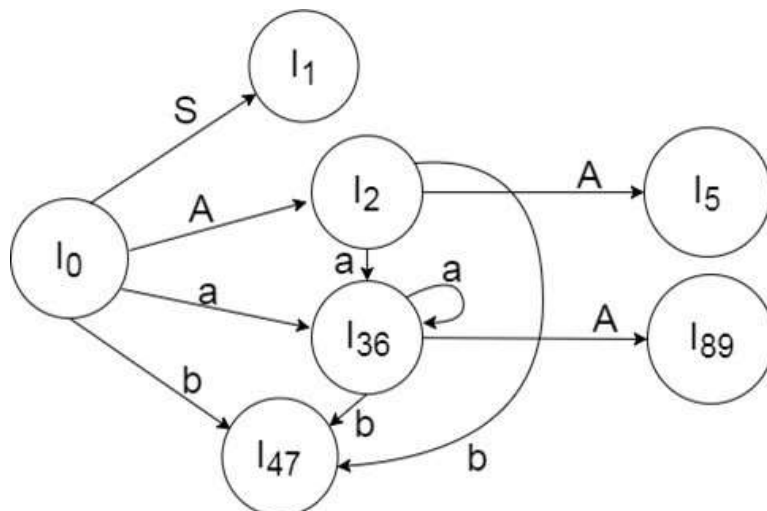
The  $I_4$  and  $I_7$  are same but they differ only in their lookahead, so we can combine them and called as  $I_{47}$ .

$I_{47} = \{ A \rightarrow b \bullet, a/b/\$ \}$

The  $I_8$  and  $I_9$  are same but they differ only in their lookahead, so we can combine them and called as  $I_{89}$ .

$I_{89} = \{ A \rightarrow a A \bullet, a/b/\$ \}$

Drawing DFA:





LALR (1) Parsing table:

States	a	b	S	S	A
I <sub>0</sub>	S <sub>36</sub>	S <sub>47</sub>		12	
I <sub>1</sub>		accept			
I <sub>2</sub>	S <sub>36</sub>	S <sub>47</sub>			5
I <sub>36</sub>	S <sub>36</sub> S <sub>47</sub>				89
I <sub>47</sub>	R <sub>3</sub> R <sub>3</sub>	R <sub>3</sub>			
I <sub>5</sub>			R <sub>1</sub>		
I <sub>89</sub>	R <sub>2</sub>	R <sub>2</sub>	R <sub>2</sub>		

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## LRPARSERS

An efficient bottom-up syntax analysis technique that can be used CFG is called LR(k) parsing. The 'L' is for left-to-right scanning of the input, the 'R' for constructing a rightmost derivation in reverse, and the 'k' for the number of input symbols. When 'k' is omitted, it is assumed to be 1.

### Advantages of LR parsing:

1. It recognizes virtually all programming language constructs for which CFG can be written.
2. It is an efficient non-backtracking shift-reduce parsing method.
3. A grammar that can be parsed using LR method is a proper superset of a grammar that can be parsed with predictive parser.
4. It detects a syntactic error as soon as possible.

### Drawbacks of LR method:

It is too much of work to construct a LR parser by hand for a programming language grammar. A specialized tool, called a LR parser generator, is needed.

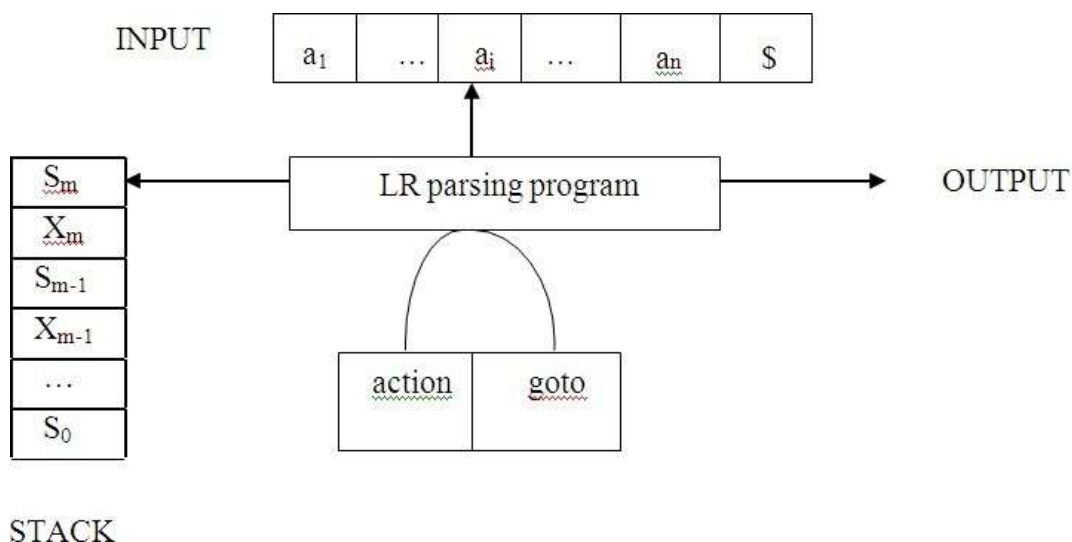
Example: YACC.

### Types of LR parsing method:

1. SLR- Simple LR  
Easiest to implement, least powerful.
2. CLR- Canonical LR  
Most powerful, most expensive.
3. LALR- Look-Ahead LR  
Intermediate in size and cost between the other two methods.

### The LR parsing algorithm:

The schematic form of an LR parser is as follows:



**Fig. 2.5 Model of an LR parser**

It consists of an input, an output, a stack, a driver program, and a pa parts (action and goto).

- ☐ The driver program is the same for all LR parser.
- ☐ The parsing program reads characters from an input buffer one at a time.
- ☐ The program uses a stack to store a string of the forms  $0X_1s_1X_2s_2\dots X_ms_m$ , where  $s_m$  is on top. Each  $X_i$  is a grammar symbol and each  $s_i$  is a state.
- ☐ The parsing table consists of two parts :action and goto functions.

**Action:** The parsing program determines  $s_m$ , the state currently on top of stack, and  $a_i$ , the current input symbol. It then consults  $action[s_m, a_i]$  in the action table which can have one of four values:

1. shift  $s$ , where  $s$  is a state,
2. reduce by a grammar production  $A \rightarrow \beta$ ,
3. accept
4. error.

**Goto :** The function goto takes a state and grammar symbol as arguments and produces a state.

**LR Parsing algorithm:**

Input: An input string  $w$  and an LR parsing table with functions action and goto for grammar  $G$ . Output: If  $w$  is in  $L(G)$ , a bottom-up-parse for  $w$ ; otherwise, an error

indication.

Method: Initially, the parser has  $s_0$  on its stack, where  $s_0$  is the initial state, and  $w\$$  in the input buffer. The parser then executes the following program:

```
set ip to point to the first input symbol of  $w\$$ ; repeat
forever begin let  $s$  be the state on top of the stack
and
    a the symbol pointed to by ip;
if  $\text{action}[s, a] = \text{shift } s'$  then begin
    push  $a$  then  $s'$  on top of the stack;
    advance ip to the next
input symbol end else if
 $\text{action}[s, a] = \text{reduce } A \rightarrow \beta$  then
begin
    pop  $2^* | \beta |$  symbols off the stack;
    let  $s'$  be the state now on top of the stack; push  $A$  then  $\text{goto}[s', A]$  on top of the stack; output
    the production  $A \rightarrow \beta$ 
end
else if  $\text{action}[s, a] =$ 
    accept then
    return
```

#### **CONSTRUCTING SLR(1) PARSINGTABLE:**

To perform SLR parsing, take grammar as input and do the following:

1. Find LR(0) items.
2. Completing the closure.
3. Compute  $\text{goto}(I, X)$ , where  $I$  is set of items and  $X$  is grammar symbol.

#### **LR(0) items:**

An LR(0) item of a grammar  $G$  is a production of  $G$  with a dot at some position of the right side. For example, production  $A \rightarrow XYZ$  yields the four items

### Closure operation:

If  $I$  is a set of items for a grammar  $G$ , then  $\text{closure}(I)$  is the set of items constructed from  $I$  by the two rules:

1. Initially, every item in  $I$  is added to  $\text{closure}(I)$ .
2. If  $A \rightarrow \alpha \cdot B \beta$  is in  $\text{closure}(I)$  and  $B \rightarrow \gamma$  is a production, then add the item  $B \rightarrow \cdot \gamma$  to  $I$ , if it is not already there. We apply this rule until no more new items can be added to  $\text{closure}(I)$ .

### Goto operation:

$\text{Goto}(I, X)$  is defined to be the closure of the set of all items  $[A \rightarrow \alpha X \cdot \beta]$  such that  $[A \rightarrow \alpha \cdot X \beta]$  is in  $I$ .

Steps to construct SLR parsing table for grammar  $G$  are:

1. Augment  $G$  and produce  $G'$
2. Construct the canonical collection of set of items  $C$  for  $G'$
3. Construct the parsing action function  $\text{action}$  and  $\text{goto}$  using the following algorithm that requires  $\text{FOLLOW}(A)$  for each non-terminal of grammar.

### Algorithm for construction of SLR parsing table:

Input : An augmented grammar  $G'$

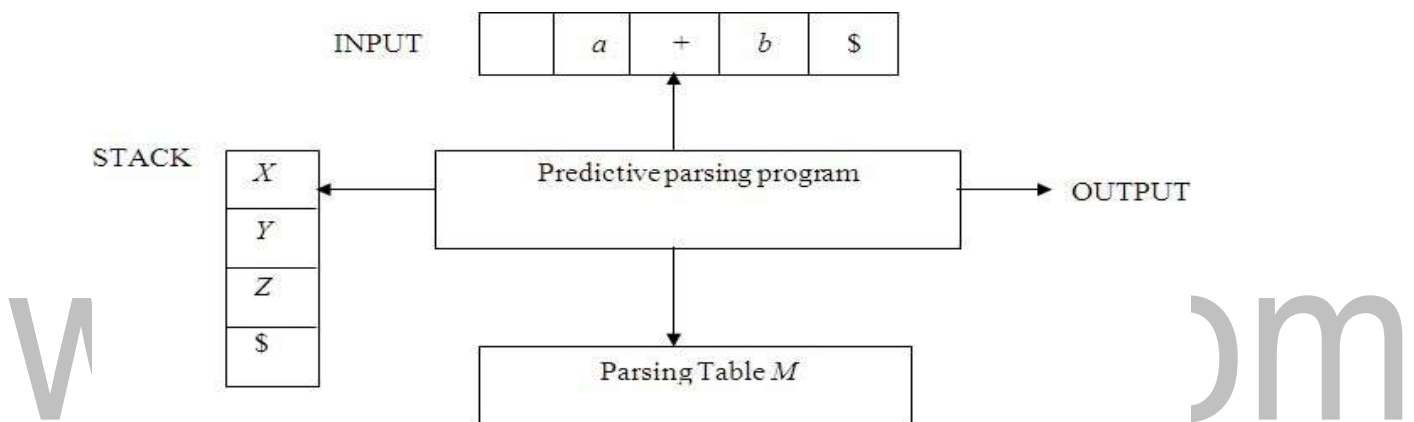
Output : The SLR parsing table functions  $\text{action}$  and  $\text{goto}$  for  $G'$

Method :

1. Construct  $C = \{I_0, I_1, \dots, I_n\}$ , the collection of sets of LR(0) items for  $G'$ .
2. State  $I$  is constructed from  $I_i$ . The parsing functions for state  $I$  are determined as follows:
  - (a) If  $[A \rightarrow \alpha \cdot a \beta]$  is in  $I_i$  and  $\text{goto}(I_i, a) = I_j$ , then set  $\text{action}[i, a]$  to "shift  $j$ ". Here  $a$  must be terminal.
  - (b) If  $[A \rightarrow \alpha \cdot]$  is in  $I_i$ , then set  $\text{action}[i, a]$  to "reduce  $A \rightarrow \alpha$ " for all  $a$  in  $\text{FOLLOW}(A)$ .
  - (c) If  $[S' \rightarrow \cdot S]$  is in  $I_i$ , then set  $\text{action}[i, \$]$  to "accept".If any conflicting actions are generated by the above rules, we say grammar is not SLR(1).
3. The  $\text{goto}$  transitions for state  $I$  are constructed for all non-term  $A$  if  $\text{goto}(I_i, A) = I_j$ , then  $\text{goto}[i, A] = j$ .
4. All entries not defined by rules (2) and (3) are made "error"
5. The initial state of the parser is the one constructed from the  $[S' \rightarrow \cdot S]$ .

## PREDICTIVE PARSING

It is possible to build a non recursive predictive parser by maintaining a stack explicitly, rather than implicitly via recursive calls. The key problem during predictive parsing is that of determining the production to be applied for a non terminal . The non recursive parser in figure looks up the production to be applied in parsing table. In what follows, we shall see how the table can be constructed directly from certain grammars.



### Model of a nonrecursive predictive parser

A table-driven predictive parser has an input buffer, a stack, a parsing table, and an output stream. The input buffer contains the string to be parsed, followed by `$`, a symbol used as a right endmarker to indicate the end of the input string. The stack contains a sequence of grammar symbols with `$` on the bottom, indicating the bottom of the stack. Initially, the stack contains the start symbol of the grammar on top of `$`. The parsing table is a two dimensional array  $M[A,a]$  where  $A$  is a non terminal, and  $a$  is a terminal or the symbol `$`. The parser is controlled by a program that behaves as follows. The program considers  $X$ , the symbol on the top of the stack, and  $a$ , the current input symbol. These two symbols determine the action of the parser. There are three possibilities.

parsing.

- 1 If  $X = a = \$$ , the parser halts and announces successful completion of

2 If  $X=a!=\$$ , the parser pops  $X$  off the stack and advances the input pointer to the next input symbol.

3 If  $X$  is a non terminal, the program consults entry  $M[X,a]$  of the parsing table  $M$ . This entry will be either an  $X$ -production of the grammar or an error entry. If, for example,  $M[X,a]=\{X \rightarrow UVW\}$ , the parser replaces  $X$  on top of the stack by  $WVU$  (with  $U$  on top). As output, we shall assume that the parser just prints the production used; any other code could be executed here. If  $M[X,a]=\text{error}$ , the parser calls an error recovery routine.

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### Algorithm for Non recursive predictive Parsing.

Input. A string  $w$  and a parsing table  $M$  for grammar  $G$ .

Output. If  $w$  is in  $L(G)$ , a leftmost derivation of  $w$ ; otherwise, an error indication.

Method. Initially, the parser is in a configuration in which it has  $\$S$  on the stack with  $S$ , the start symbol of  $G$  on top, and  $w\$$  in the input buffer. The program that utilizes the predictive parsing table  $M$  to produce a parse for the input is shown in Fig.

set  $ip$  to point to the first symbol of  $w\$$ .

repeat

let  $X$  be the top stack symbol and  $a$  the symbol pointed to by  $ip$ . if  $X$  is

a terminal of  $\$$  then

if  $X=a$  then

pop  $X$  from the stack and advance  $ip$

else error()

else

if  $M[X,a]=X \rightarrow Y_1Y_2\dots Y_k$  then begin

pop  $X$  from the stack;

push  $Y_k, Y_{k-1}, \dots, Y_1$  onto the stack, with  $Y_1$  on top;

output the production  $X \rightarrow Y_1Y_2\dots Y_k$

end

else error()

until  $X=\$$  /\* stack is empty\*/

### Predictive parsing table construction:

The construction of a predictive parser is aided by two functions associated with a grammar  $G$  :

1. FIRST
2. FOLLOW

### Rules for first( ):



1. If  $X$  is terminal, then  $FIRST(X)$  is  $\{X\}$ .
2. If  $X \rightarrow \epsilon$  is a production, then add  $\epsilon$  to  $FIRST(X)$ .
3. If  $X$  is non-terminal and  $X \rightarrow a\alpha$  is a production then add  $a$  to  $FIRST(X)$ .
4. If  $X$  is non-terminal and  $X \rightarrow Y_1 Y_2 \dots Y_k$  is a production, then place  $a$  in  $FIRST(X)$  if for some  $i$ ,  $a$  is in  $FIRST(Y_i)$ , and  $\epsilon$  is in all of  $FIRST(Y_1), \dots, FIRST(Y_{i-1})$ ; that is,  $Y_1, \dots, Y_{i-1} \Rightarrow \epsilon$ . If  $\epsilon$  is in  $FIRST(Y_j)$  for all  $j=1, 2, \dots, k$ , then add  $\epsilon$  to  $FIRST(X)$ .

**Rules for follow ( ):**

1. If  $S$  is a start symbol, then  $FOLLOW(S)$  contains  $\$$ .
2. If there is a production  $A \rightarrow \alpha B \beta$ , then every thing in  $FIRST(\beta)$  except  $\epsilon$  is placed in  $follow(B)$ .
3. If there is a production  $A \rightarrow \alpha B$ , or a production  $A \rightarrow \alpha B \beta$  where  $FIRST(\beta)$  contains  $\epsilon$ , then everything in  $FOLLOW(A)$  is in  $FOLLOW(B)$ .

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### Algorithm for construction of predictive parsing table:

Input : Grammar G Output

: ParsingtableMMMethod:

1. For each production  $A \rightarrow \alpha$  of the grammar, do steps 2 and 3.
2. For each terminal  $a$  in  $FIRST(\alpha)$ , add  $A \rightarrow \alpha$  to  $M[A, a]$ .
3. If  $\epsilon$  is in  $FIRST(\alpha)$ , add  $A \rightarrow \alpha$  to  $M[A, b]$  for each terminal  $b$  in  $FOLLOW(A)$ . If  $\epsilon$  is in  $FIRST(\alpha)$  and  $\$$  is in  $FOLLOW(A)$ , add  $A \rightarrow \alpha$  to  $M[A, \$]$ .
4. Make each undefined entry of  $M$  be error.

Example:

Consider the following grammar :

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow (E) \mid id$

After eliminating left-recursion the grammar is  $E$

$\rightarrow TE'$

$E' \rightarrow +TE' \mid \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' \mid \epsilon$

$F \rightarrow (E) \mid id$

First( ) :

$FIRST(E) = \{ (, id \}$

$FIRST(E') = \{ +, \epsilon \}$

$FIRST(T) = \{ (, id \}$

$FIRST(T') = \{ *, \epsilon \}$

$FIRST(F) = \{ (, id \}$

Follow( ) :  $FOLLOW(E) = \{$

$\$, ) \}$

$FOLLOW(E') = \{ \$, ) \}$

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$\text{FOLLOW}(T) = \{ +, \$, ) \}$

$\text{FOLLOW}(T') = \{ +, \$, ) \}$

$\text{FOLLOW}(F) = \{ +, *, \$, ) \}$

**Predictive parsing Table**

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NON-TERMINAL	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

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stack	Input	Output
SE	<u>id</u> +id*id \$	
SE'T	<u>id</u> +id*id \$	E → TE'
SE'T'F	<u>id</u> +id*id \$	T → FT'
SE'T'id	<u>id</u> +id*id \$	F → id
SE'T'	+id*id \$	
SE'	+id*id \$	T' → ε
SE'T+	+id*id \$	E' → +TE'
SE'T	id*id \$	
SE'T'F	id*id \$	T → FT'
SE'T'id	id*id \$	F → id
SE'T'	*id \$	
SE'T'F*	*id \$	T' → *FT'
SE'T'F	id \$	
SE'T'id	id \$	F → id
SE'T'	\$	
SE'	\$	T' → ε
\$	\$	E' → ε

### Stack Implementation

LL(1) grammar:

The parsing table entries are single entries. So each location has not more than one entry. This type of grammar is called LL(1) grammar.

Consider the following grammar:

$$S \rightarrow iEtS \mid iEtSeS \mid a$$

$$E \rightarrow b$$

After eliminating left factoring, we have

$$S \rightarrow iEtSS' \mid a$$

$$S' \rightarrow eS \mid \epsilon$$

$$E \rightarrow b$$

To construct a parsing table, we need FIRST() and FOLLOW() for all the non-

$$\text{FIRST}(S) = \{ i, a \}$$

$$\text{FIRST}(S') = \{ e, \epsilon \}$$

$$\text{FIRST}(E) = \{ b \}$$

$$\text{FOLLOW}(S) = \{ \$, e \}$$

$$\text{FOLLOW}(S') = \{ \$, e \}$$

$$\text{FOLLOW}(E) = \{ t \}$$

NON-TERMINAL	a	b	e	i	t	S
S	<u><math>S \rightarrow a</math></u>			<u><math>S \rightarrow iEtSS'</math></u>		
S'			$S' \rightarrow eS$ $S' \rightarrow \epsilon$			$S' \rightarrow \epsilon$
E		<u><math>E \rightarrow b</math></u>				

**Parsing table:**

Since there are more than one production, the grammar is not

LL(1) grammar. Actions performed in predictive parsing:

1. Shift
2. Reduce
3. Accept
4. Error

**Implementation of predictive parser:**

1. Elimination of left recursion, left factoring and ambiguous grammar.
2. Construct FIRST() and FOLLOW() for all non-terminals.
3. Construct predictive parsing table.
4. Parse the given input string using stack and parsing table.

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## SYNTAX ANALYSIS

Syntax analysis is the second phase of the compiler. It gets the input from the tokens and generates a syntax tree or parse tree.

Advantages of grammar for syntactic specification :

1. A grammar gives a precise and easy-to-understand syntactic specification of a programming language.
2. An efficient parser can be constructed automatically from a properly designed grammar.
3. A grammar imparts a structure to a source program that is useful for its translation into object code and for the detection of errors.
4. New constructs can be added to a language more easily when there is a grammatical description of the language.

### 2.1 THE ROLE OF PARSER

The parser or syntactic analyzer obtains a string of tokens from the lexical analyzer and verifies that the string can be generated by the grammar for the source language. It reports any syntax errors in the program. It also recovers from commonly occurring errors so that it can continue processing its input.

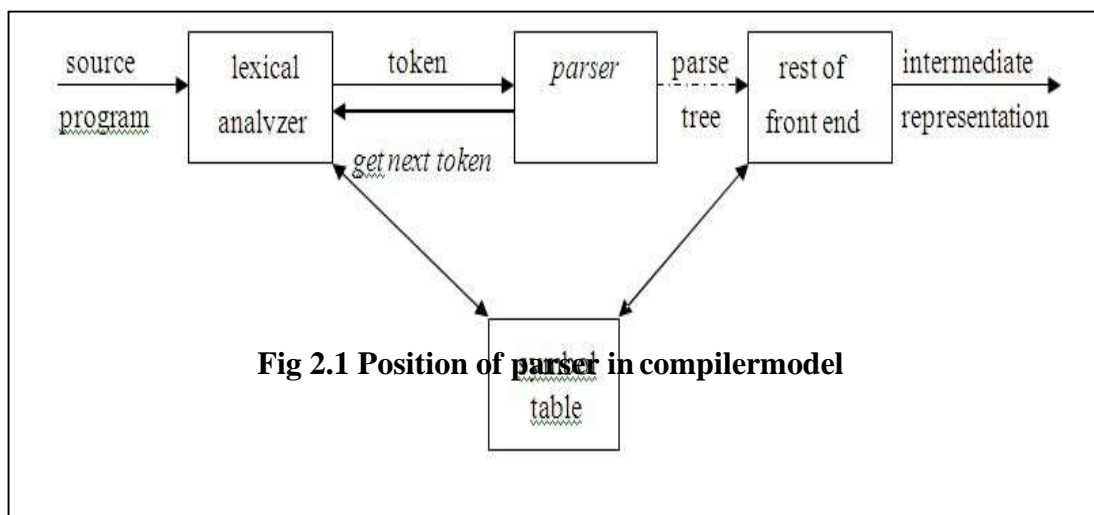


Fig 2.1 Position of parser in compiler model

Position of parser in compiler model



**Functions of the parser :**

1. It verifies the structure generated by the tokens based on the grammar.
2. It constructs the parse tree.
3. It reports the errors.
4. It performs error recovery.

**Issues :**

Parser cannot detect errors such as:

1. Variable re-declaration
2. Variable initialization before use.
3. Data type mismatch for an operation.

The above issues are handled by Semantic Analysis phase.

**Syntax error handling :**

Programs can contain errors at many different levels. For example :

1. Lexical, such as misspelling an identifier, keyword or operator.
2. Syntactic, such as an arithmetic expression with unbalanced parentheses.
3. Semantic, such as an operator applied to an incompatible operand.
4. Logical, such as an infinitely recursive call.

**Functions of error handler :**

1. It should report the presence of errors clearly and accurately.
2. It should recover from each error quickly enough to be able to detect subsequent errors.
3. It should not significantly slow down the processing of correct programs.

**Error recovery strategies :**

The different strategies that a parser uses to recover from a syntactic error are:

1. Panic mode
2. Phrase level
3. Error productions
4. Global correction

### **Panic mode recovery:**

On discovering an error, the parser discards input symbols one at a time until semicolon or end. It has the advantage of simplicity and does not go into an infinite loop. When multiple errors in the same statement are rare, this method is quite useful.

### **Phrase level recovery:**

On discovering an error, the parser performs local correction on the remaining input that allows it to continue. Example: Insert a missing semicolon or delete an extraneous semicolon etc.

### **Error productions:**

The parser is constructed using augmented grammar with error productions. If an error production is used by the parser, appropriate error diagnostics can be generated to indicate the erroneous constructs recognized by the input.

### **Global correction:**

Given an incorrect input string  $x$  and grammar  $G$ , certain algorithms can be used to find a parse tree for a string  $y$ , such that the number of insertions, deletions and changes of tokens is as small as possible. However, these methods are in general too costly in terms of time and space.